# Frames

منشات تستخدم لتغطیة بحور من اکثر من ۱۲م وتتمیز بان لها عمق (depth) اقل وترخیم اقل (deflection) مقارنة به (Main girders)

## -Types of Frames

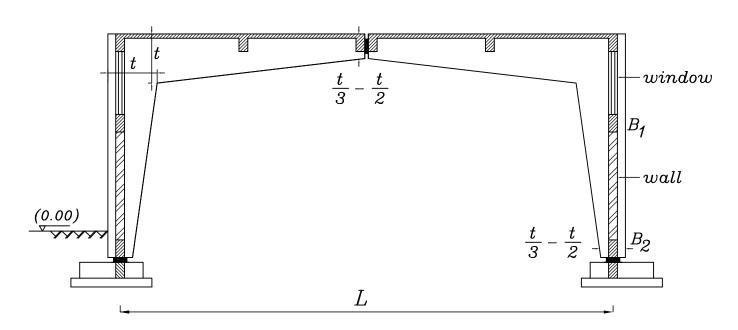
1-Three hinged Frame.

2-Two hinged frame.

3-Fixed Frame.

4-Cantilever Frame.

5-Continuous Frame.



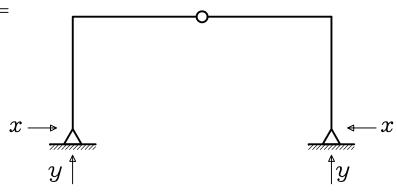
- Three hinged Frame is usually used For spans  $(12 \rightarrow 20m)$
- It is better for weak soil [ determinate structure].

#### -Concrete Dimensions

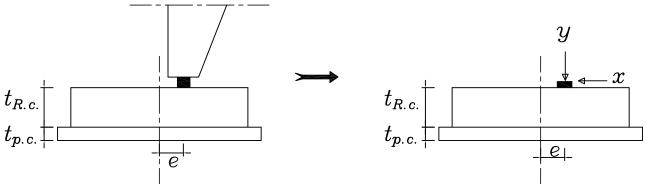
$$t=rac{L}{10}$$
 ايهما اكبر $b=rac{30\ cm}{rac{spacing}{20}}$ 



#### -Statical System



نقوم بترحيل قواعد(Frame) للخارج مسافة (e) لضمان توزيع الاجهادات بانتظام على التربة  $(uniform\ stress)$ 



Moment due to vertical reaction (y) =Moment due to hzReaction(x)

$$y^*e = x(t_{R.c.} + t_{p.c.}) \qquad \longrightarrow \qquad e = \frac{x(t_{R.c.} + t_{p.c.})}{y}$$

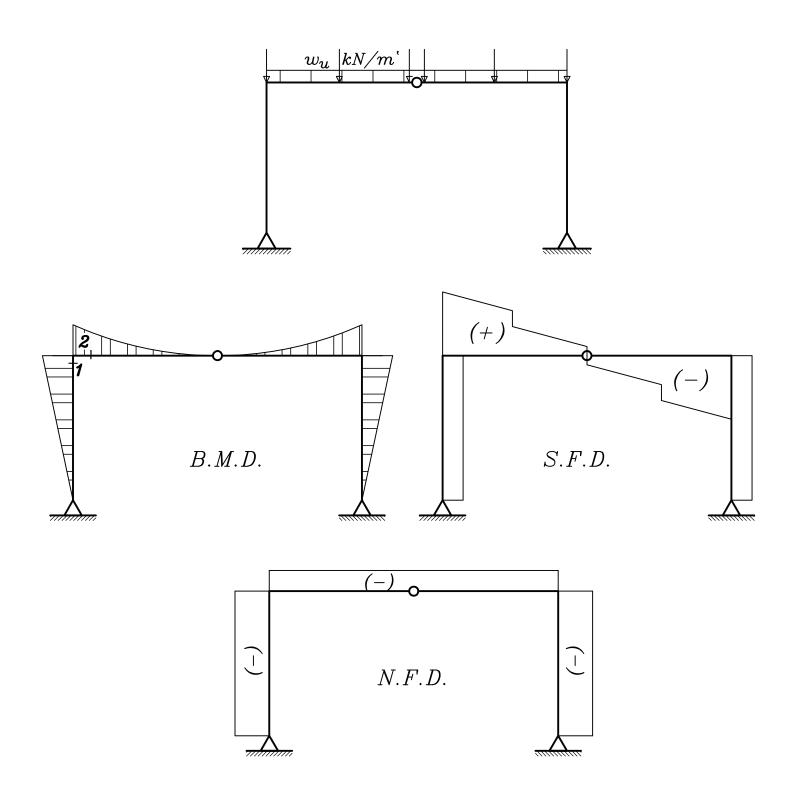
### -Steps of design

1-Get the loads on Secondary beams from load distribution and get their reactions on the frame.

2-Get the distributed loads on the frame.

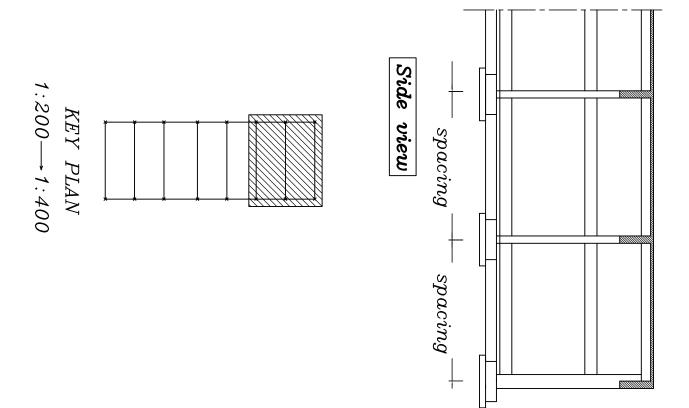
$$w = \gamma_c b(t-t_s) *1.40 + \frac{\Sigma Area}{span} w_s$$

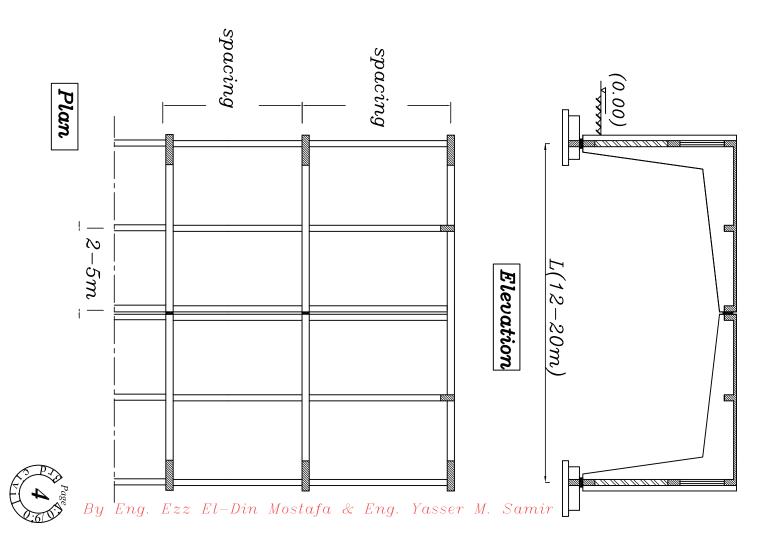
 $3-\ Draw\ B.M.D$  , N.F.D. , S.F.D. of the Frame

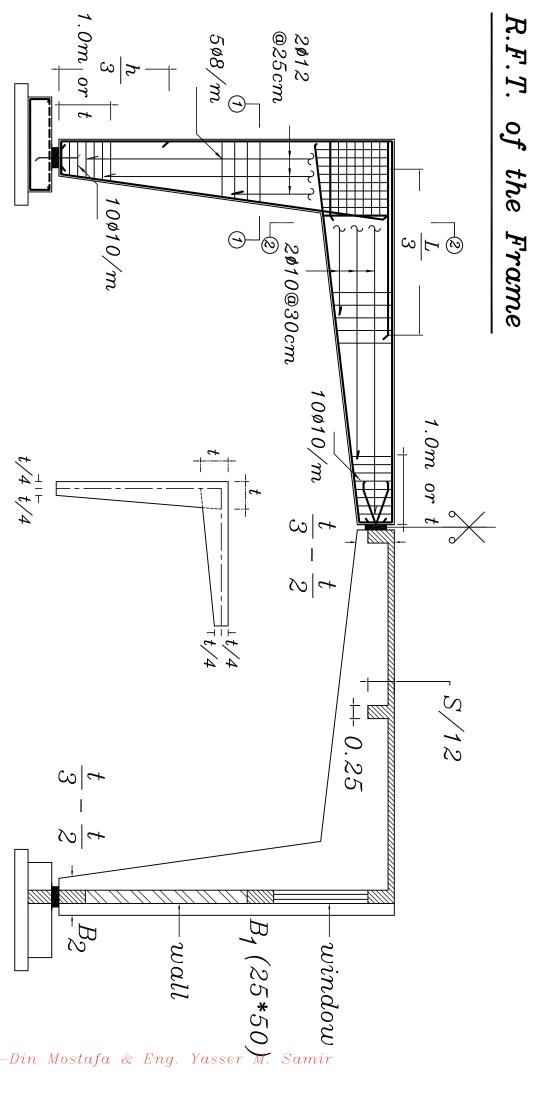


4-Design section ( 1-1), (2-2) and get Rft.

ملحوظة  $(B_1,B_2)$  للحظ ان الكمرات  $(B_1,B_2)$  فائدتها ما يلى  $(B_1,B_2)$  تقلل  $(B_1)$  الكمرة  $(B_1)$  نقلل  $(B_1)$  الكمرة  $(B_1)$  تتحمل الحائط و تقوم بتربيط ال  $(B_2)$  ببعضها  $(B_2)$  تتحمل الحائط و تقوم بتربيط ال

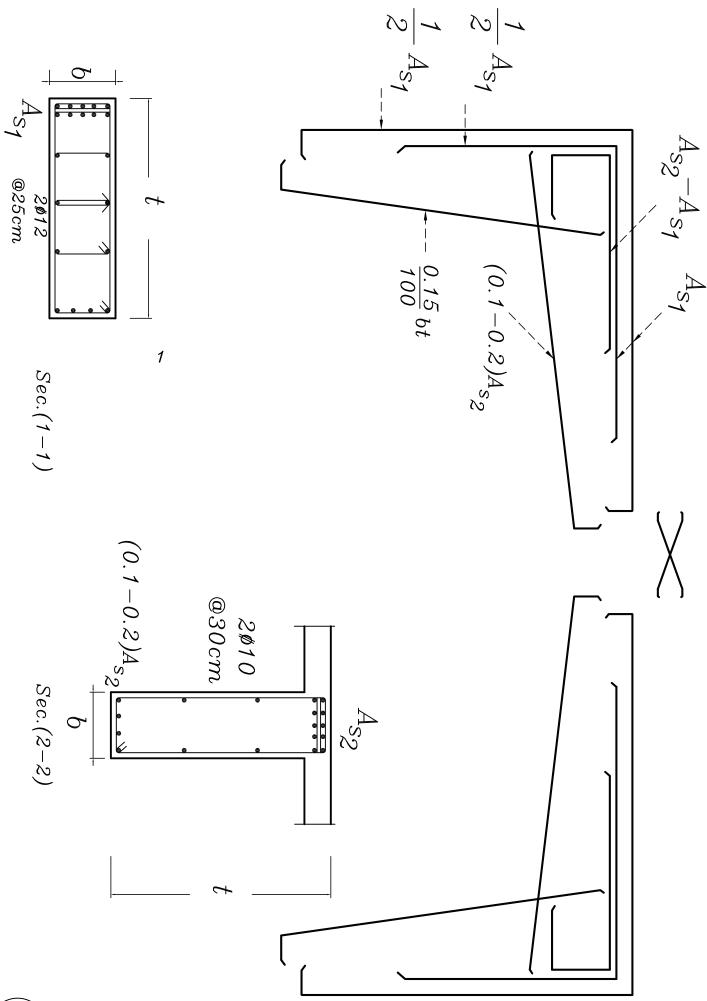








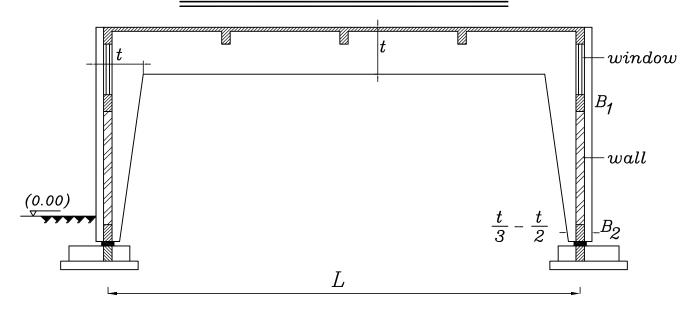
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## Two Hinged Frame

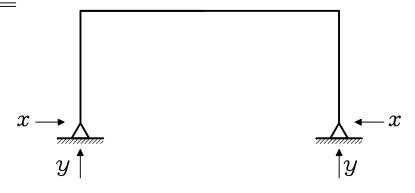


- Two Hinged Frame is used for span (12  $\rightarrow$  25)

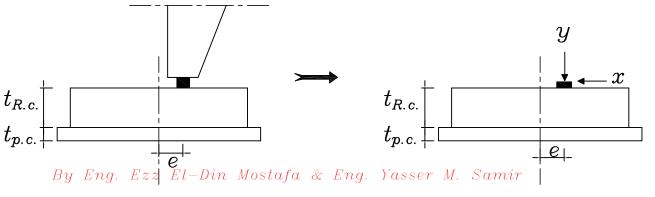
#### -Concrete Dimensions

$$t=rac{L}{12-14}$$
  $b=\left[egin{array}{cc} 30 & cm \ spacing \ \hline 20 \end{array}
ight]$  ایها اکبر

#### -Statical System



نقوم بترحيل قواعد(Frame) للخارج مسافة (e) لضمان توزيع الاجهادات بانتظام على التربة  $(uniform\ stress)$ 



Moment due to vertical reaction (y) = Moment due to hzReactin(x)

$$y^*e = x(t_{R.c.} + t_{p.c.}) \qquad \qquad = \frac{x(t_{R.c.} + t_{p.c.})}{y}$$

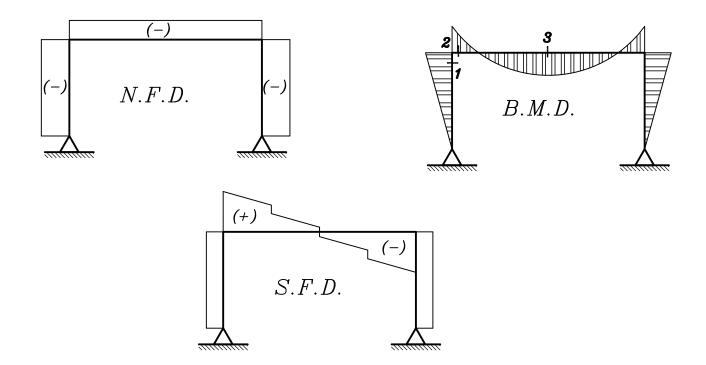
# Steps of design

- 1-Get the loads on the secondary beams from load distribution and get their reactions on the frame.
- 2-Get the distributed load on the frame.

$$w_u = \gamma_c b(t-t_s) *1.40 + \frac{\sum Area}{span} w_s$$

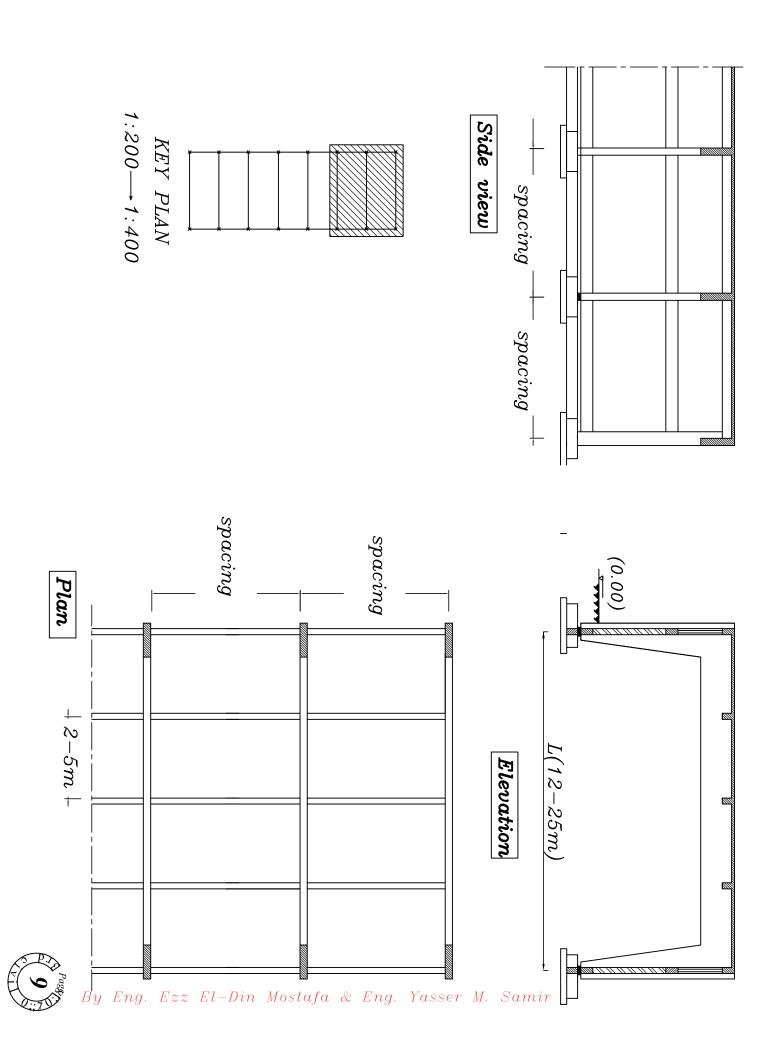
- 3-Solve the frame using virtual work Method

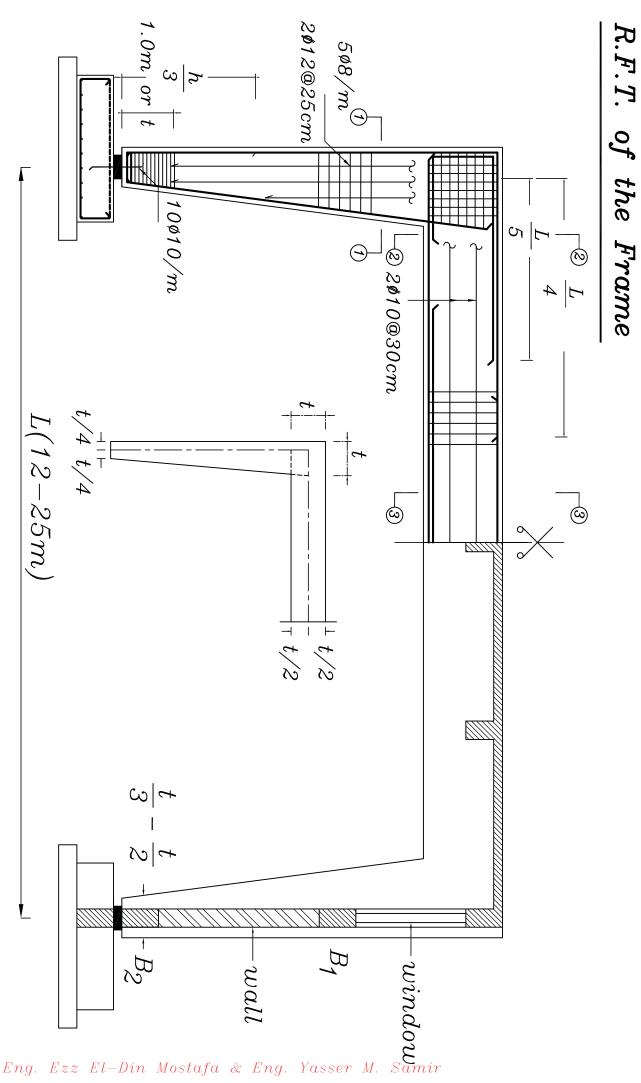
  OR Moment Distribution Method.
- 4- Draw B.M.D , N.F.D. , S.F.D.



5-Design sections (1-1),(2-2),(3-3) and get rft.

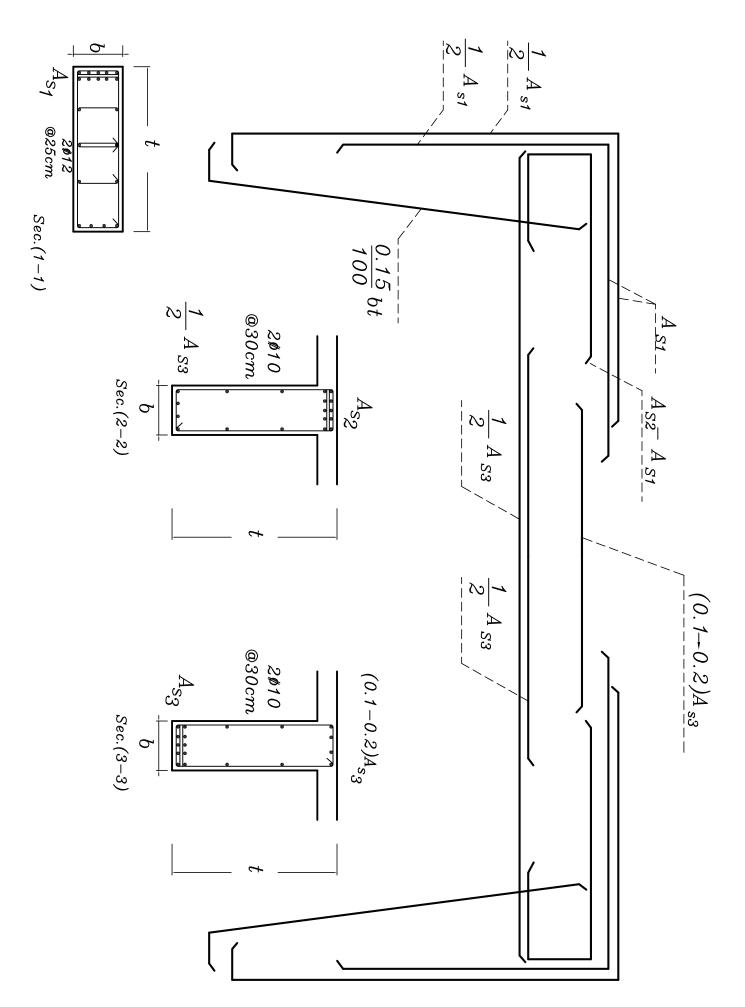






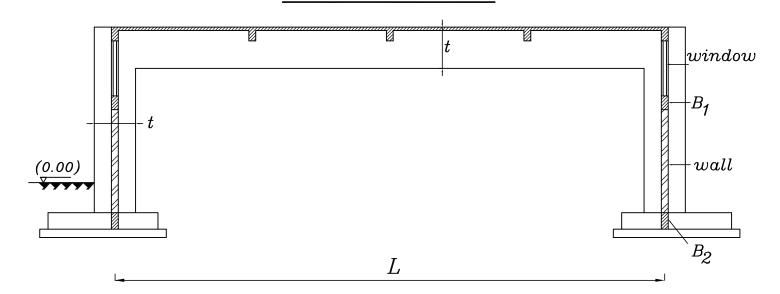


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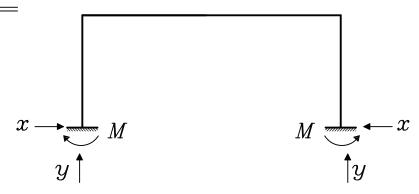
## Fixed Frame



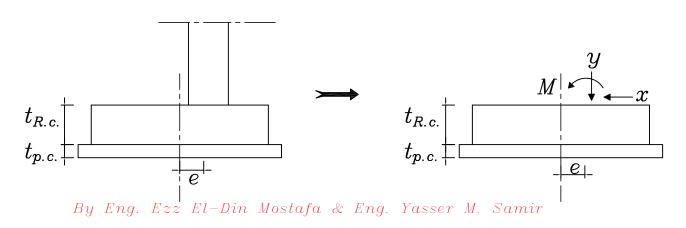
## -Concrete Dimensions

$$t=rac{L}{14-16}$$
  $b=\left[egin{array}{c} 30 \ cm \ spacing \ \hline 20 \ \end{array}
ight.$  ایها اکبر

#### -Statical System



نقوم بترحيل قواعد(Frame) للخارج مسافة (e) لضمان توزيع الاجهادات بانتظام على التربة  $(uniform\ stress)$ 





Moment due to vertical reaction (y) = Moment due to hzReactin(x)+Moment due to (M)

$$y*e=x(t_{R.c.}+t_{p.c.})+M$$
  $\longrightarrow$   $e=\frac{x(t_{R.c.}+t_{p.c.})+M}{y}$ 

## Steps of design

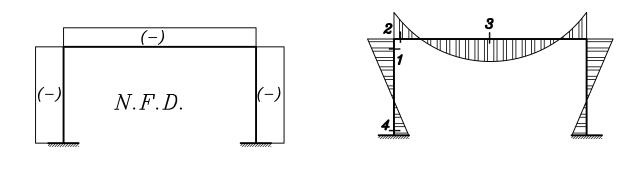
- 1-Get the loads on the secondary beams from load distribution and get their reactions on the frame.
- 2-Get the distributed load on the frame.

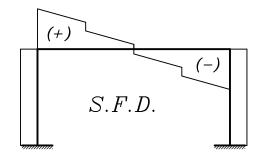
$$w_u = \gamma_c b(t-t_s) *1.40 + \frac{\sum Area}{span} w_s$$

3-Solve the frame using virtual work Method

OR Moment Distribution Method.

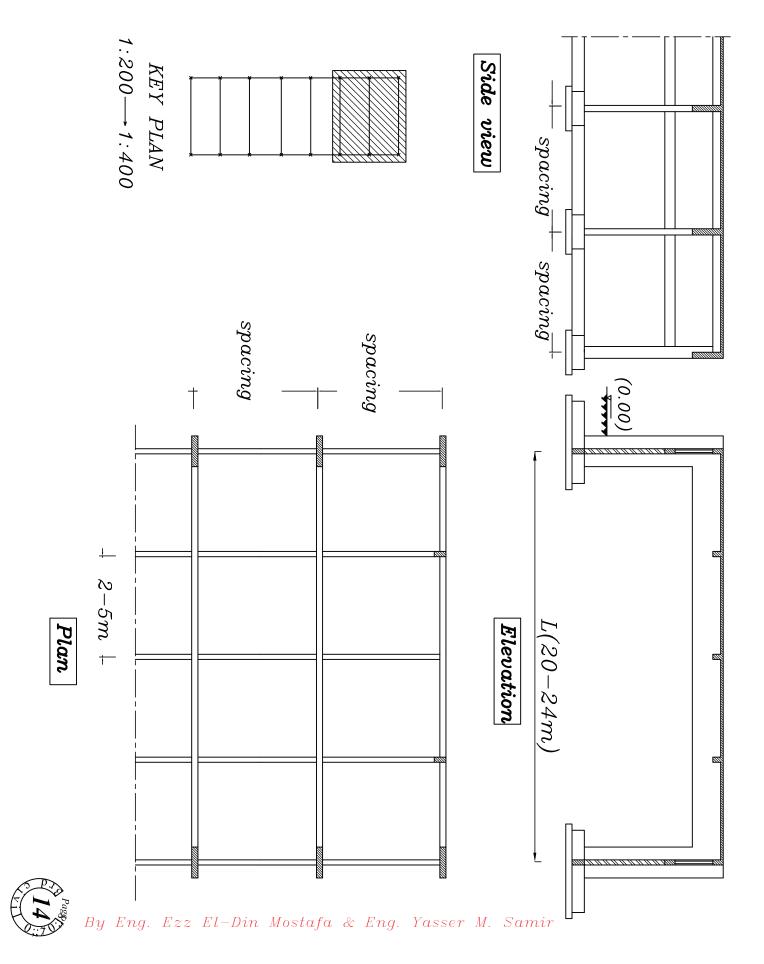
4- Draw B.M.D , N.F.D. , S.F.D.

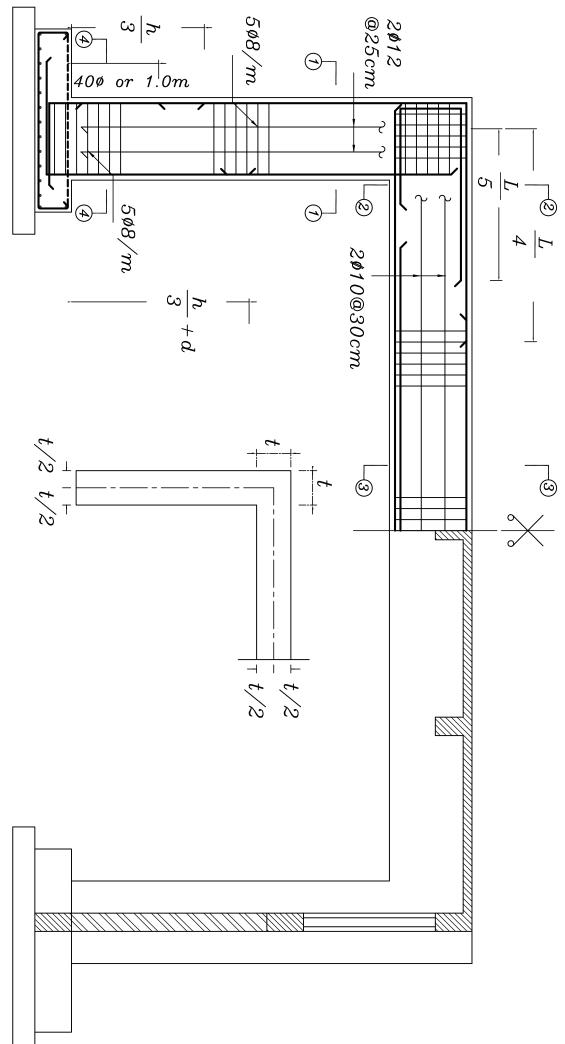




5-Design sections (1-1),(2-2),(3-3),(4-4) and get rft.

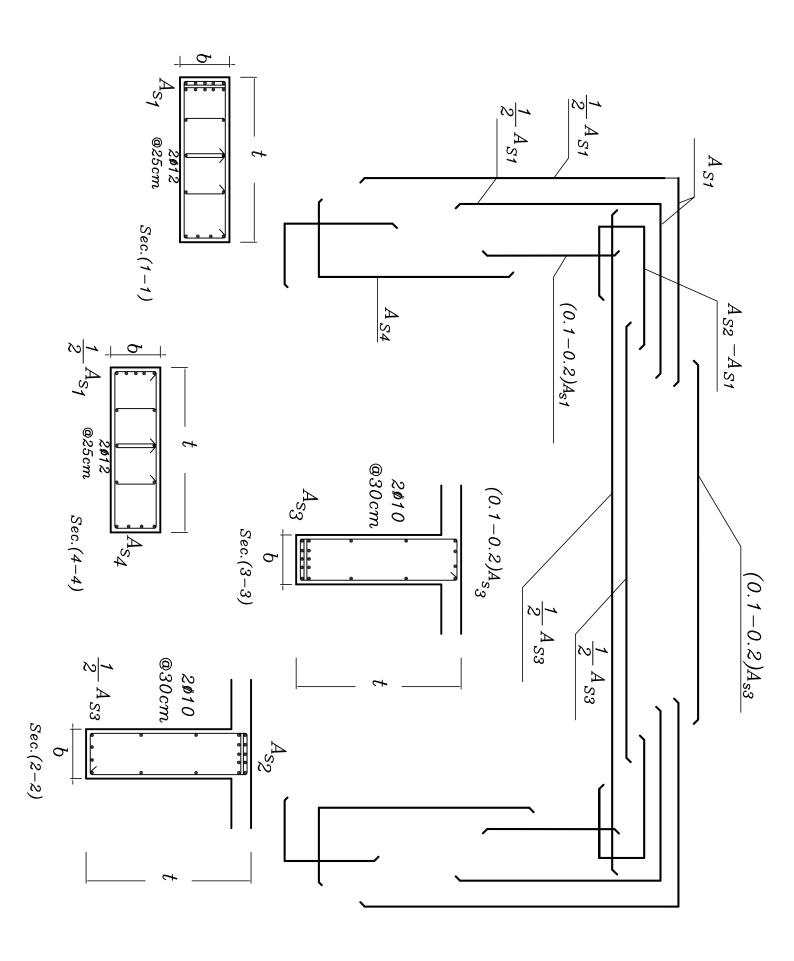








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# Solved examples on frames

# Example

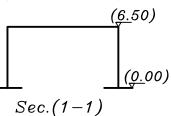
For the given plan and cross- section,



it is required to:

1- Draw structural plan and cross section to show all concrete elements.

2- Design the slabs and Main supporting given



$$f_{cu} = 27.5 N/mm^2$$
  $f_y = 360 N/mm^2$ 

$$f_{y} = 360 N / mm^{2}$$

$$F.C. = 1.5kN/m^2$$
  $L.L. = 1.0kN/m^2$ 

$$L.L.=1.0kN/m^2$$

# Solution

## 1-Design for solid slabs:

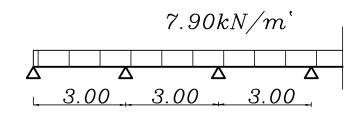
$$t_{\rm s} = \frac{L_{\rm s}}{24} = \frac{300}{24} = 12.50cm$$

take  $t_s = 12cm$  for all slabs (check deflection)

$$w_{su} = 1.4(t_s \gamma_c + F.C.) + 1.6L.L.$$

$$=1.4[0.12*25+1.5]+1.6*1.0$$

$$w_{su} = 7.90 \ kN/m^2$$



## Design of strip

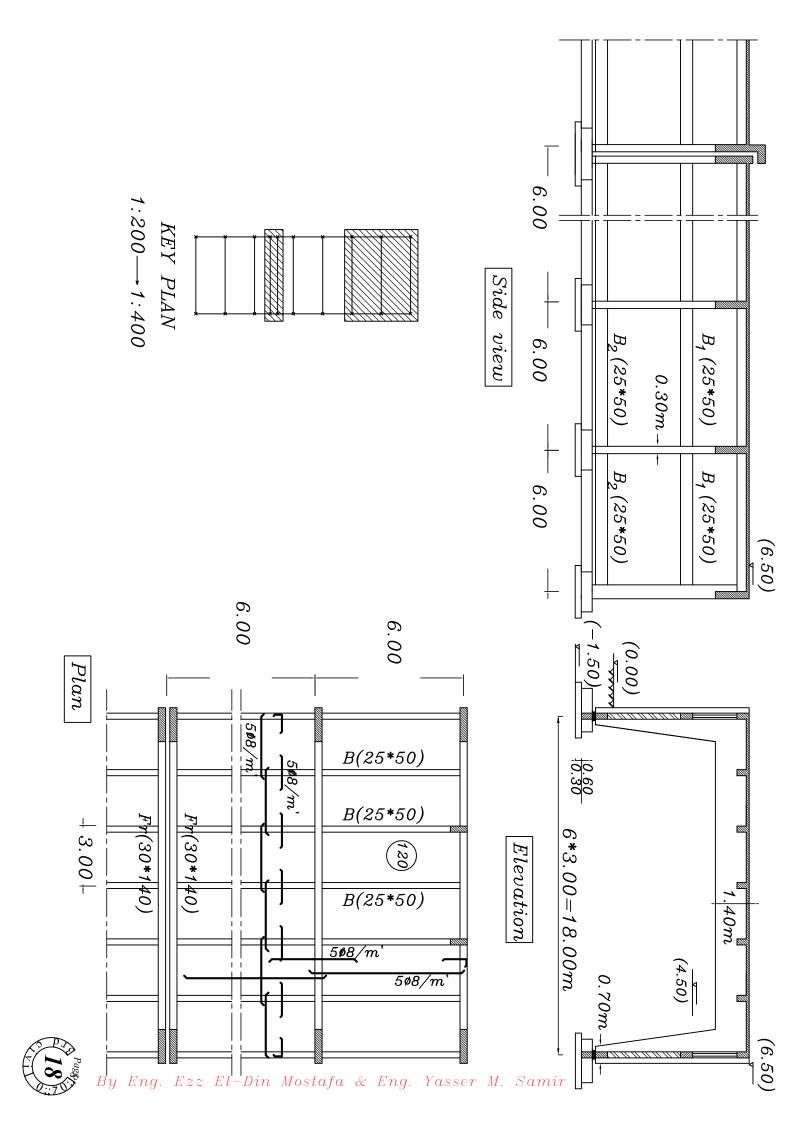
Sec. (1-1)

$$100 = C_1 \sqrt{\frac{7.11*10^6}{1000*27.5}} C_1 = 6.22$$
,  $J = 0.826$ 

$$A_{s} = \frac{7.11*10^{6}}{0_{By}82_{Eng.}^{6*1}0_{Ezz}^{0*360}} = 239 \text{ mm}^{2}$$

$$= 239 \text{ mm}^{2}$$





## 2- Design for secondary beams

#### For $B_1$

$$w_1 = \gamma_c b(t - t_s) * 1.4 + w_s \frac{L_s}{2}$$

$$w_1 = 25*0.25(0.5-0.12)*1.40+7.9*\frac{3.0}{2}$$

$$w_1 = 15.18kN/m$$

$$R_1 = w_1 * Spacing$$

$$R_1 = 15.18*6 = 91.05kN$$

## For $B_2$

$$w_2 = \gamma_c b(t - t_s) * 1.4 + w_s . L_s$$

$$w_2 = 25*0.25(0.5-0.12)*1.40+7.9*3.0$$

$$w_2 = 27.03kN/m$$

$$R_2 = w_2 * Spacing$$

$$R_2 = 27.03*6 = 162.15kN$$

#### 3-Design of Main System

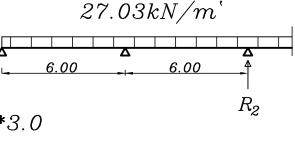
assume 
$$b=30cm$$
 ,  $t=\frac{L}{12-14}=\frac{18}{12-14}=1.40m$ 

$$w_{eq} = 0.w + \frac{\sum P}{L}$$

$$w_{eq} = 25*0.3*(1.4-0.12)*1.40+\frac{162.15*5+91.05*2}{18}$$

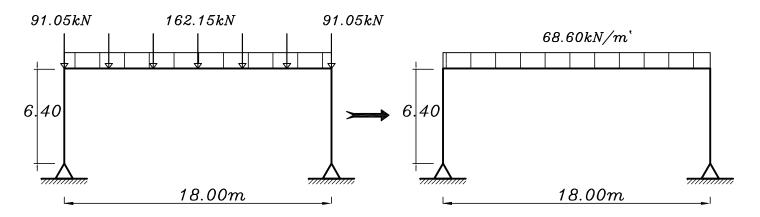
$$w_{eq} = 68.60 \text{ kN/m}^{\circ}$$

$$h = 6.50 + 1.50 - 0.30 - 0.60 - \frac{1.40}{2} = 6.40m$$
  
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15.18kN/m'





$$I_b = 349*10^{-4}*1.02*1.4^3$$

$$I_{b} = 0.098m^{4}$$

$$I_c = \frac{B(\frac{5}{6}t)^3}{12} = \frac{0.3*(\frac{5}{6}*1.40)^3}{12}$$

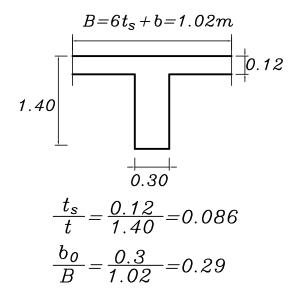
$$I_c = 0.0397m^4$$

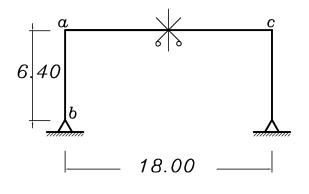
#### For Joint a

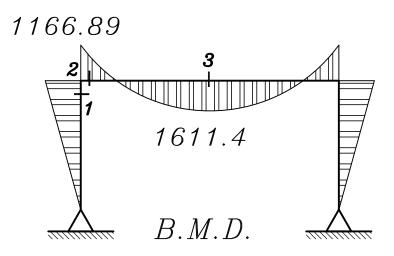
$$D.f_{ab} = \frac{0.75(I_c/h)}{(0.75\frac{I_c}{h}) + (0.5\frac{I_b}{L})}$$

$$D.f_{ab} = \frac{0.75*(0.0397/6.40)}{0.75*(0.0397/6.40)+0.50*(0.098/18)}$$

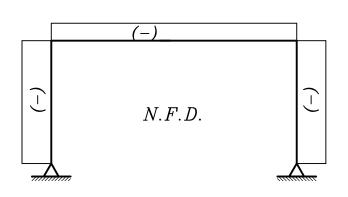
$$D.f_{ab} = 0.63$$

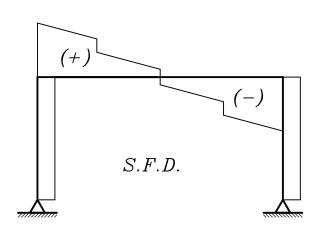












### Design of Sections

**Sec.** (1-1) 
$$M_{u.l.} = 1166.89kN.m$$

$$N_{u,l} = 617.64kN.m$$

$$b=300mm$$
 ,  $t=1400mm$ 

$$t = 1400 mm$$

$$\frac{N_{u.l.}}{btf_{cu}} = \frac{617.64*10^3}{300*1400*27.5} = 0.05>0.04 \text{ (Dont neglect } N_{u.l.} \text{)}$$

$$e = \frac{M_{u.l.}}{N_{u.l.}} = \frac{1166.89}{617.64} = 1.89m$$

$$\frac{e}{t} = \frac{1.89}{1.40} = 1.35 > 0.5$$
 (big eccentricity)

$$e_s = e + \frac{t}{2} - c = 1.89 + \frac{1.40}{2} - 0.1 = 2.49m$$

$$M_{us} = 617.64 * 2.49 = 1537.9 kN.m$$

$$d = C_1 \sqrt{\frac{Mus}{b*f_{cu}}}$$

$$1300 = C_1 \sqrt{\frac{1537.9*10^6}{300*27.5}} \qquad C_1 = 3.01 \& J = 0.752$$

$$C_1 = 3.01 \& J = 0.752$$

$$A_s = \frac{Mus}{J.d.f_y} - \frac{Nus}{f_y/\gamma_s}$$

$$A_s = \frac{1537.9*10^6}{0.752*1300*360} - \frac{617.64*10^3}{360/1.15}$$

$$A_s = 24 cm^2 = 7022$$

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Sec. 
$$(2-2)$$

Sec. (2-2)  $M_{u,l} = 1166.89kN.m$   $N_{u,l} = 209.81kN.m$ 

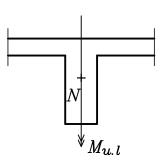
$$b=300mm$$
 ,  $t=1400mm$ 

$$\frac{N_{u.l.}}{btf_{cu}} = \frac{209.81*10^3}{300*1400*27.5} = 0.018<0.04 \ (neglect\ N_{u.l.})$$

$$d = C_1 \sqrt{\frac{Mu.l.}{b * f_{cu}}}$$

$$1300 = C_1 \sqrt{\frac{1166.89*10^6}{300*27.5}} \qquad C_1 = 3.46 \& J = 0.778$$

$$C_1 = 3.46 \& J = 0.778$$



$$A_s = \frac{1166.89*10^6}{0.778*1300*360}$$

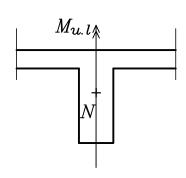
$$A_s = 32.05 cm^2 = 9 / 22$$

Sec. 
$$(3-3)$$

Sec. (3-3)  $M_{u.l.} = 1611.4kN.m$   $N_{u.l.} = 209.81kN.m$ 

$$b=300mm$$
 ,  $t=1400mm$ 

$$\frac{N_{u.l.}}{btf_{m.}} = \frac{209.81*10^{3}}{300*1400*27.5} = 0.018<0.04 \ (neglect\ N_{u.l.})$$



B = 2220mm

$$d=C_1\sqrt{\frac{Mu.l.}{B*f_{cu}}}$$

$$1300 = C_1 \sqrt{\frac{1611.4*10^6}{2220*27.5}}$$
  $C_1 = 8.0 \& J = 0.826$ 

$$C_1 = 8.0 \& J = 0.826$$

$$A_s = \frac{1611.4*10^6}{0.826*1300*360}$$

$$A_s = 4 \text{ B.} 68 \text{ cm}^2 \text{ E} = 9 \text{ D.} 25 \text{ in Mostafa & Eng. Yasser M. Samir}$$



#### Check Shear

$$\begin{split} Q_{cr} &= Q_{max} - w(\frac{c}{2} + \frac{d}{2}) \\ Q_{cr} &= 526.59 - 58.51(\frac{1.40}{2} + \frac{1.30}{2}) \\ Q_{cr} &= 447.60kN \\ q_{su} &= \frac{Q_{cr}}{bd} = \frac{447.60*10^3}{300*1300} = 1.15 \ N/mm^2 \\ q_{cu} &= 0.24\sqrt{\frac{27.5}{1.5}} = 1.03 \ N/mm^2 \end{split}$$

 $q_{cu} < q_u < q_{umax}$ 

$$q_{max} = 0.7 \sqrt{\frac{27.5}{1.5}} = 3.00 \ N/mm^2$$

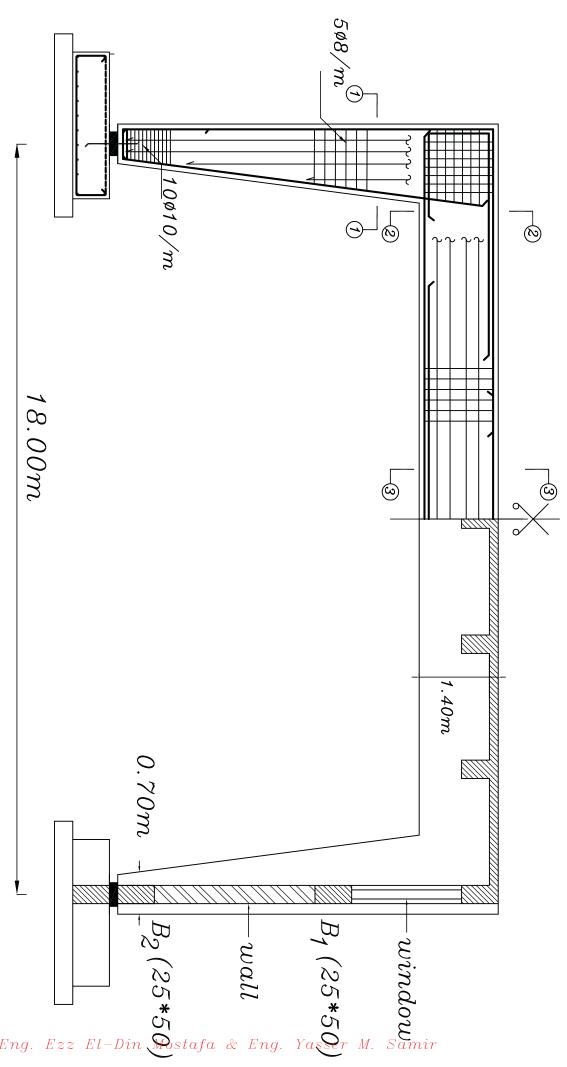
$$q_u - \frac{q_{cu}}{2} = \frac{nA_s f_y / \gamma_s}{bS}$$

assume 
$$n=2$$

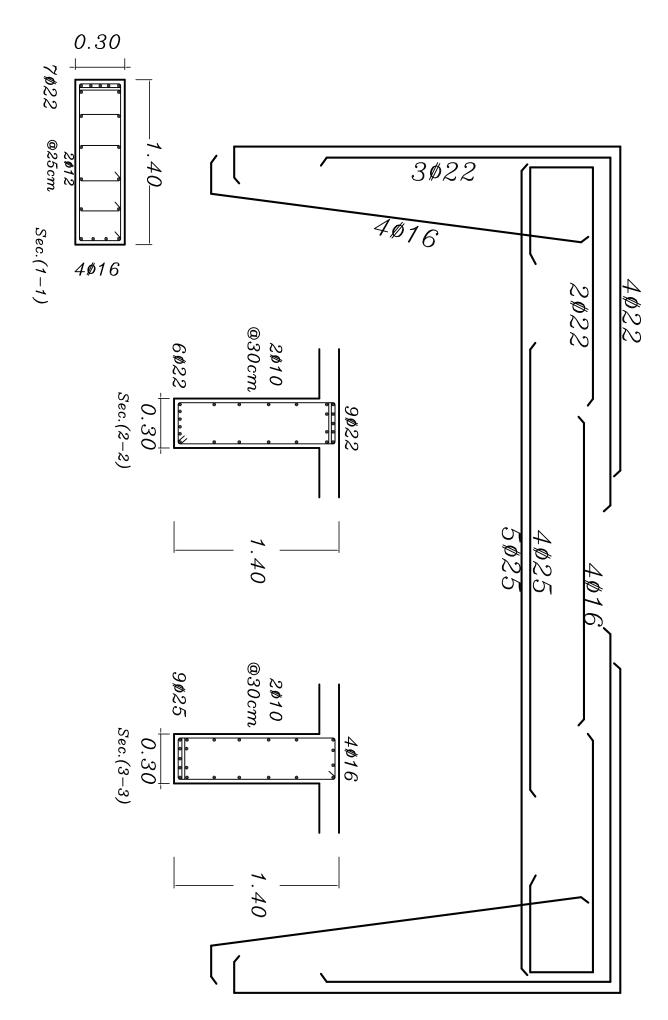
$$A_{S} = 78.5 mm^{2} = \emptyset 10$$

$$1.15 - \frac{1.03}{2} = \frac{2*78.5*240/1.15}{300*S} \implies S = 172mm$$

No. of 
$$stirrups/m' = \frac{1000}{S} = 5.8$$
 Take Stirrups 6010/m'









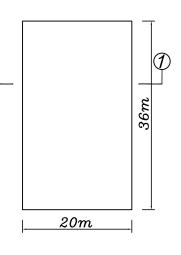
## Example

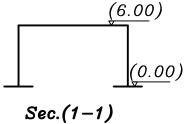
For the given plan and cross- section, Columns are only allowed on the outside perimeter

#### it is required to:

- 1- Draw structural plan and Elevation to show all concrete elements.
- 2- Design the slabs and Main supporting element.

$$O.W.(blocks)=0.15 \ kN/block$$





# given

$$f_{cu} = 30N/mm^2 f_y = 360N/mm^2 F.C. = 1.5kN/m^2$$
  
 $L.L. = 2.0kN/m^2$ 

# Solution

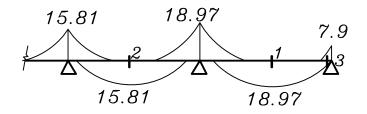
## For one way H.B. Slabs.

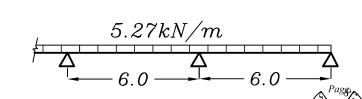
assume 
$$t=250mm$$
 &  $t_s=50mm$  &  $h=200mm$ 

$$w_{u,l} = 1.4(t_s \gamma_c + f.c. + 2bh\gamma_c + 10*wt.of Block) + 1.6 L.L$$

$$w_{u,l} = 1.4(0.05*25+1.5+2*0.1*0.2*25+10*0.15)+1.6*2.0$$

$$w_{u.l} = 10.55 \text{ kN/m}$$
  $w_{rib} = 5.27 \text{kN/m}$ 





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## Design of Sections.

Sec. (1-1) 
$$M_{u.l.} = 18.97kN.m$$
  $d=250-30=220mm$ 

$$d = C_1 \sqrt{\frac{M_{u.l.}}{f_{cu*b}}}$$
  $220 = C_1 \sqrt{\frac{18.97*10^6}{30*500}}$ 

$$C_1 = 6.2$$
  
 $J = 0.826$ 

$$A_{s} = \frac{M_{u.l.}}{J f_{u} d} = \frac{18.97*10^{6}}{360*0.826*220} = 290 \text{mm}/\text{rib}$$

1*\$12+1\$16/rib* 

Sec. (2-2) 
$$M_{u.l.} = 15.81 \, kN. m$$

$$d = C_1 \sqrt{\frac{M_{u.l.}}{f_{cu*b}}}$$
  $220 = C_1 \sqrt{\frac{15.81*10^6}{30*500}}$ 

$$C_1 = 6.8$$
  
 $J = 0.826$ 

$$A_{s} = \frac{M_{u.l.}}{J f_{u} d} = \frac{15.81*10^{6}}{360*0.826*220} = 242 \text{mm}^{2}/\text{rib}$$

1*\$12+1\$16/rib* 

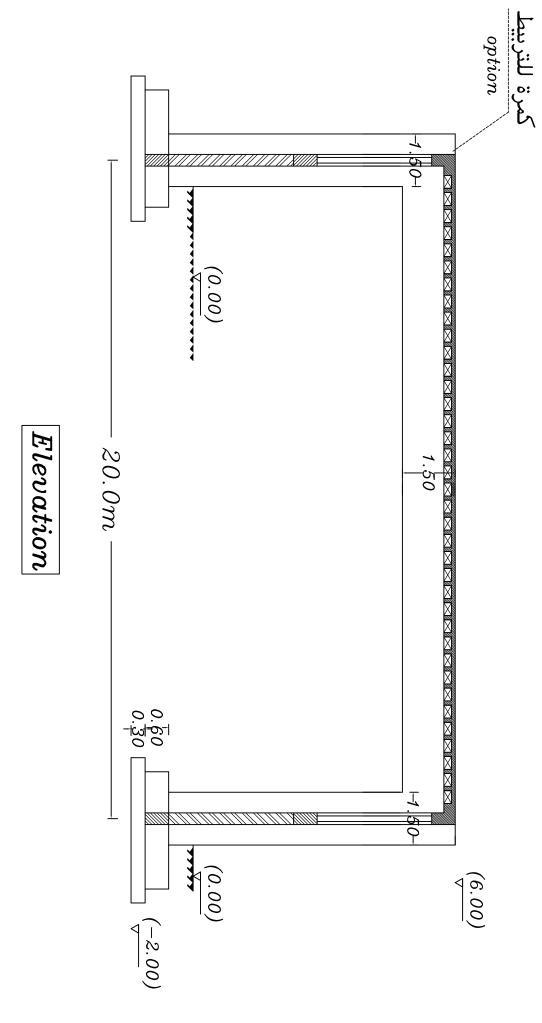
Sec. (3-3) 
$$M_{u.l.} = 7.9kN.m$$

$$d = C_1 \sqrt{\frac{M_{u.l.}}{f_{cu*b}}} \qquad 220 = C_1 \sqrt{\frac{7.9*10^6}{30*500}}$$

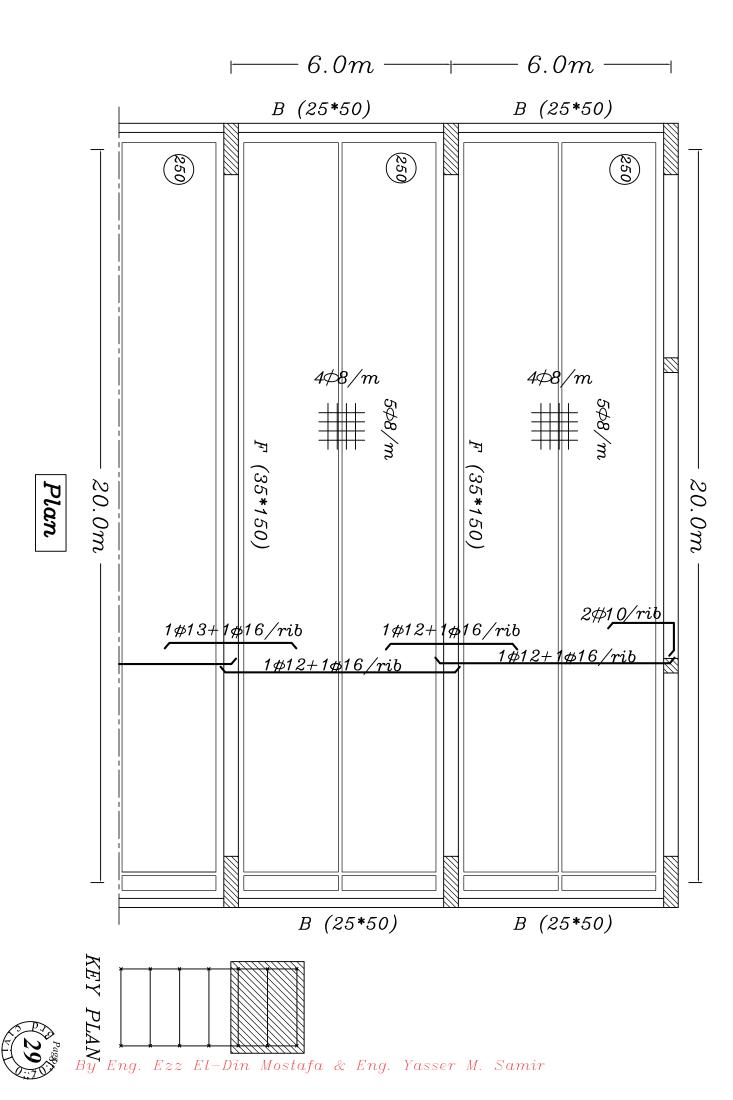
$$C_1 = 9.5$$
  
 $J = 0.826$ 

$$A_{s} = \frac{M_{u.l.}}{J f_{u} d} = \frac{7.9*10^{-6}}{360*0.826*220} = 121 \text{mm}^{2}/\text{rib}$$

2#10/rib







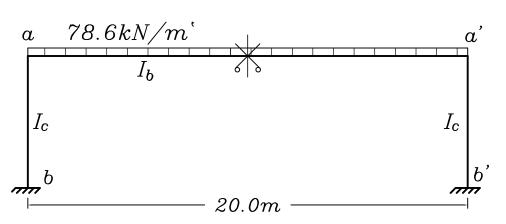
## Design of Main System

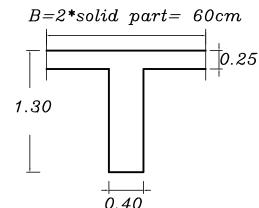
Assume 
$$b=35cm$$
 ,  $t=\frac{L}{14-16} = 1.5m$ 

$$w = 0.w + w_s *S$$

$$0.w. = 25*0.35(1.5-0.25)*1.40=15.3kN/m$$

$$w = 10.55*6+15.3 = 78.6 \ kN/m$$





## Relative Stiffness, D.F.

$$\frac{I_b}{\frac{I_b}{t}} = \frac{0.25}{1.5} = 0.17 \quad Old \\
\frac{b}{B} = \frac{0.35}{0.6} = 0.58$$

$$\frac{b}{B} = \frac{0.35}{0.6} = 0.58$$

$$I_b = 600*10^{-4}*0.6*1.5^3 = 0.121 m^4$$

$$\underline{I_c}$$
  $I_c = \frac{bt^3}{12} = \frac{0.35*1.5}{12}^3 = 0.098 m^4$ 

$$K_{ab} = \frac{I_c}{h} = \frac{0.098}{6.35} = 0.015$$

 $\hat{C}$ لاحظ ان هذا الارتفاع يقاس من girder ال C.L.

$$K_{aa} = \frac{1}{2} \frac{I_b}{L} = \frac{1}{2} * \frac{0.121}{20.0} = 0.003$$

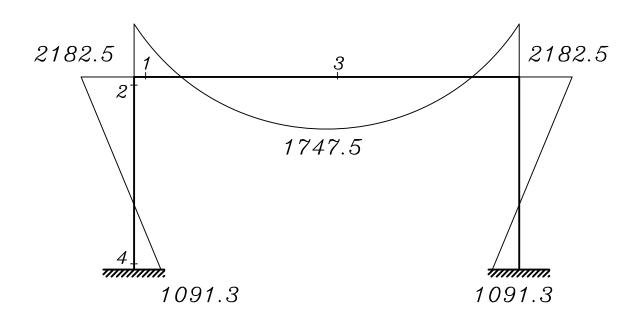
$$D.F_{ab} = \frac{K_{ab}}{K_{ab} + K_{ac}} = \frac{0.015}{0.015 + 0.003} = 0.833$$



#### Fixed End Moment

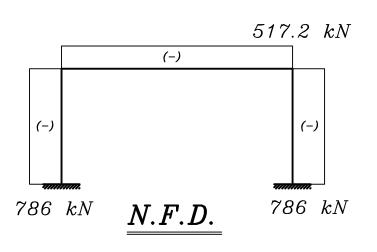
$$M = \frac{wL^2}{12} = \frac{78.6 *20^2}{12} = 2620 \ kN.m$$

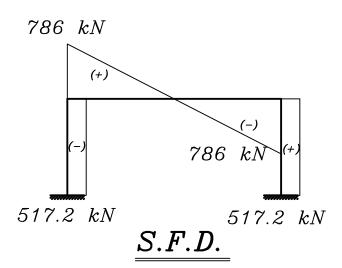
## B.M.D.



$$\therefore X=517.2 \ kN$$

$$\therefore Y = \frac{\Sigma Loads}{2} = \frac{78.6*20}{2} = 786 \ kN$$







Sec(1-1): R-Sec  $M_{u.l.} = 2182.5kN.m$ , d=1400, b=350mm $N_{u.l} = 517.2 kN$ 

$$\frac{N_{u.l.}}{f_{cu}^* bt} = \frac{517.2*10^3}{30*350*1400} = 0.035>0.04 \qquad (neglect N.F.)$$

$$d = C_1 \sqrt{\frac{Mu.l.}{b * f_{cu}}}$$

$$1400 = C_1 \sqrt{\frac{2182.5*10^6}{350*30}} \qquad C_1 = 3.07 \quad J = 0.75$$

$$A_{s} = \frac{2182.5*10^{6}}{0.75*1400*360}$$

$$A_s = 5773 mm^2$$

12\psi25

Sec(2-2): R-Sec  $M_{u.l.}$ =2182.5kN.m , d=1400 , b=350mm  $N_{u.l.}$ =786 kN

$$\frac{N_{u.l.}}{f_{cu}^* bt} = \frac{786*10^3}{30*350*1400} = 0.053>0.04 \qquad (use N.F.)$$

$$e = \frac{M_{u.l.}}{N_{u.l.}} = \frac{2182.5}{786} = 2.78m$$
  $\frac{e}{t} = \frac{2.78}{1.5} = 1.85 > 0.5$ 

⇒ Big ecc.

$$e_s = e + \frac{t}{2} - c$$
 = 2.78 +  $\frac{1.5}{2}$  - 0.1 = 3.43 m

$$M_{us} = N_{u.l.} * e_s = 786 * 3.43 = 2696 kN.m$$

$$d = C_1 \sqrt{\frac{M_{us}}{f_{cu} b}} \quad 1400 = C_1 \sqrt{\frac{2696*10^6}{30*350}} \qquad C_1 = 2.78$$



$$A_{\rm S} = \frac{M_{\rm us}}{f_{\rm y}\,J\,d} - \frac{N_{\rm u.\,l.}}{f_{\rm y}/\gamma_{\rm S}}$$

$$A_s = \frac{2696*10^6}{360*0.71*1400} - \frac{786*10^3}{360/1.15} = 5023 \text{ mm}^2$$

check Asmin

11ø25

$$A_{\text{smin}} = \frac{1.1}{f_y} bd = 1711 \text{ mm}^2$$

$$Sec(3-3)$$
:  $T-Sec$   $M_{u.l.} = 1747.5kN.m$ ,  $d=1400$ 

$$N_{u.l.} = 517.2 \ kN$$
  $B = 600mm$ 

 $Neglect N_{ul}$ 

$$1400 = C_1 \sqrt{\frac{1747.5*10^6}{600*30}} \implies C_1 = 4.49 \quad J = 0.82$$

$$A_s = \frac{1747.5*10^6}{0.82*1400*360} = 4228mm^2$$

9ø25

Sec(4-4): R-Sec  $M_{u.l.} = 1091.3kN.m$ , d=1400, b=350mm

$$N_{u.l.} = 786 \ kN$$

$$\frac{N_{u.l.}}{F_{cu}*bt} = \frac{786*10^3}{30*350*1400} = 0.053>0.04$$
 (use N.F.)

$$e = \frac{M_{u.l.}}{N_{u.l.}} = \frac{1091.3}{786} = 1.39m$$
  $\frac{e}{t} = \frac{1.39}{1.5} = 0.93$ 

⇒ Big ecc.

$$e_s = e + \frac{t}{2} - c$$
 = 1.39 +  $\frac{1.5}{2}$  - 0.1 = 2.04 m

$$M_{us} = N_{u.l.} * e_s = 786 * 2.04 = 1603 kN.m$$

$$d = C_1 \sqrt{\frac{M_{us}}{f_{cu} b}} \quad 1400 = C_1 \sqrt{\frac{1603*10^6}{30*350}} \qquad C_1 = 3.58$$

$$A_{\rm S} = \frac{M_{\rm us}}{f_{\rm y}\,J\,d} - \frac{N_{\rm u.\,l.}}{f_{\rm y}/\gamma_{\rm S}}$$

$$A_{s} = \frac{1603*10^{6}}{360*0.78*1400} - \frac{786*10^{3}}{360/1.15} = 1566 \text{ mm}^{2}$$

check Asmin

5ø22

$$A_{smin} = \frac{1.1}{f_y} bd = 1497 \text{ mm}^2 0.K.$$

#### Check Shear

$$Q_{cr} = Q_{max} - w(\frac{c}{2} + \frac{d}{2})$$

$$Q_{cr} = 786 - 78.6(\frac{1.40}{2} + \frac{1.30}{2})$$

$$Q_{cr} = 679.9kN$$

$$q_{su} = \frac{Q_{cr}}{bd} = \frac{679.9*10^3}{350*1400} = 1.39 \text{ N/mm}^2$$

$$q_{cu} = 0.24 \sqrt{\frac{30}{1.5}} = 1.07 \text{ N/mm}^2$$

 $q_{cu} < q_u < q_{umax}$ 

$$q_{max} = 0.7 \sqrt{\frac{30}{1.5}} = 3.13 \text{ N/mm}^2$$

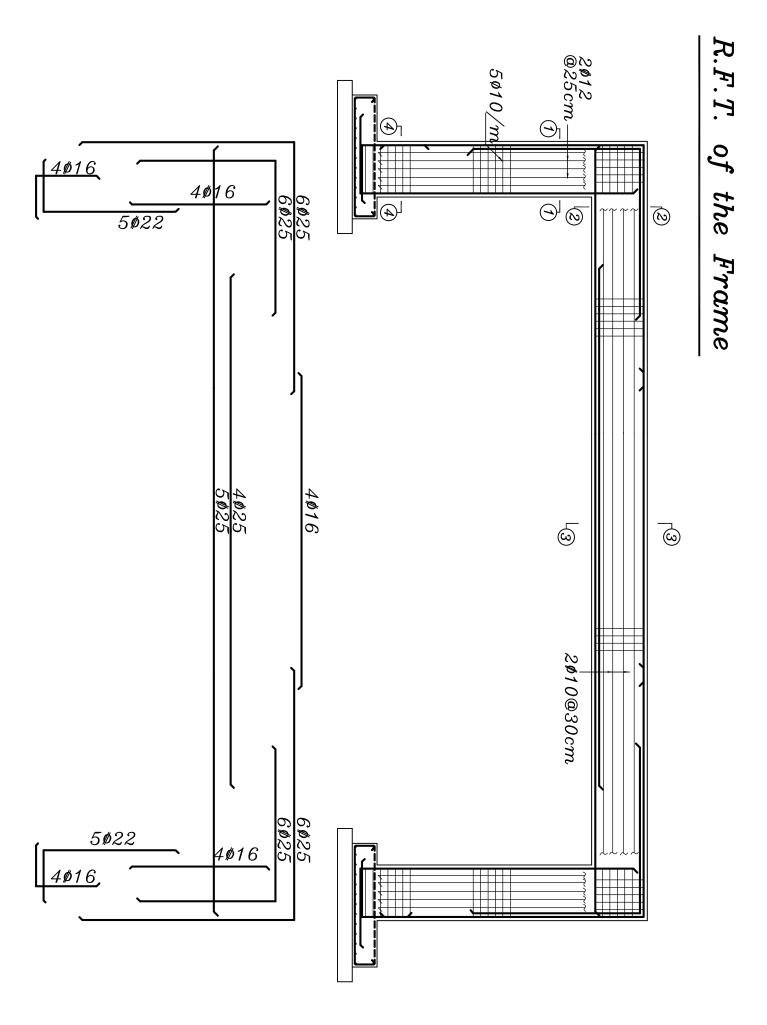
$$q_u - \frac{q_{cu}}{2} = \frac{nA_s f_y / \gamma_s}{bS}$$

assume 
$$n=2$$

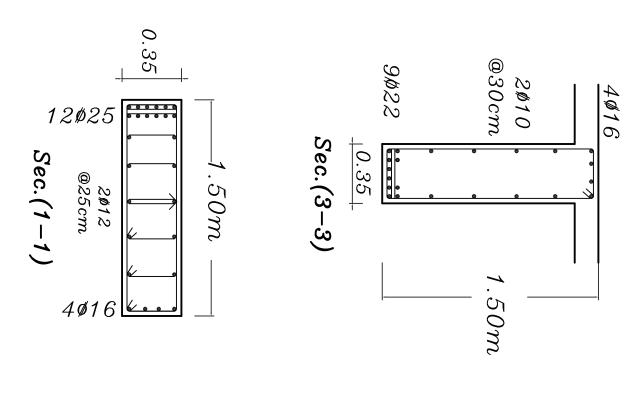
$$A_{s} = 78.5 mm^{2} = \emptyset 10$$

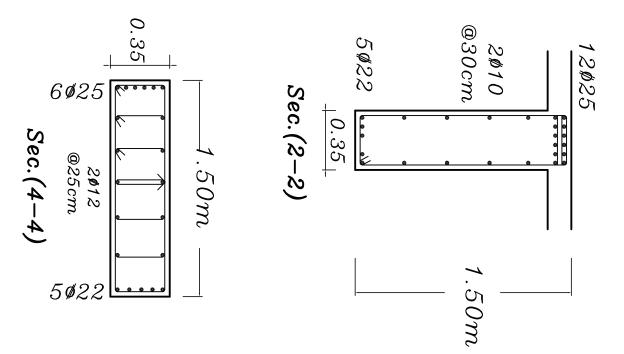
$$1.39 - \frac{1.07}{2} = \frac{2*78.5*240/1.15}{350*S} \implies S = 109mm$$

No. of  $stirrups/m' = \frac{1000}{S} = 9.1$  Take Stirrups 10010/m'











For the given plan and cross- section,

#### it is required to:

1 - Draw structural plan and cross

section to show all concrete elements.

2- Design the main supporting elements.

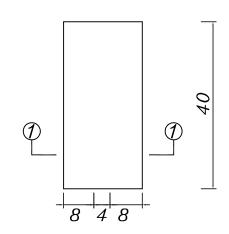
given Use all Sec. Beams 25\*50

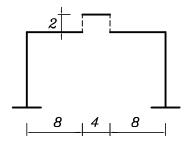
$$f_{cu}$$
= $25N/mm^2$ 

$$f_{cu} = 25N/mm^2$$
  $f_y = 360N/mm^2$ 

$$F.C. = 1.5kN/m^2$$
  $L.L. = 1.0kN/m^2$ 

$$L.L.=1.0kN/m^2$$





Sec.(1-1)

 $clear\ height=5.5m$ 

#### Solution

$$t_s = \frac{400}{40} = 10cm$$
 For sky light  $t_s = \frac{400}{35} = 11.43cm$ 

Take  $t_s = 10cm$  For all slabs except sky light,

 $take\ t_s = 12cm$ 

For 
$$t_s = 12cm$$
  $w_{su} = 1.4[t_s \gamma_c + F.c.] + 1.6 L.L.$ 

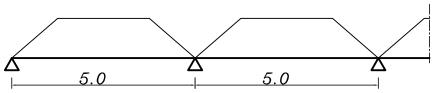
$$w_{su} = 1.4[0.12*25+1.5]+1.6*1=7.91kN/m^2$$

For 
$$t_s = 10cm$$
  $w_{su} = 1.4[0.10*25+1.5]+1.6*1=7.2kN/m^2$ 

### 1-Analysis of Beams

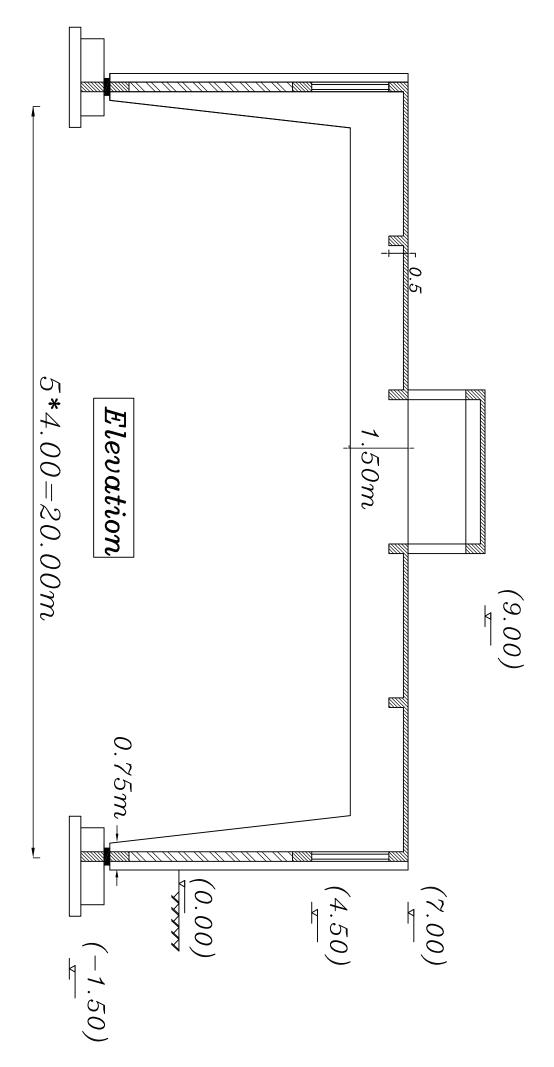
#### For $B_1$

$$C_{\alpha} = 1 - \frac{1}{2} * \frac{4}{5} = 0.60$$



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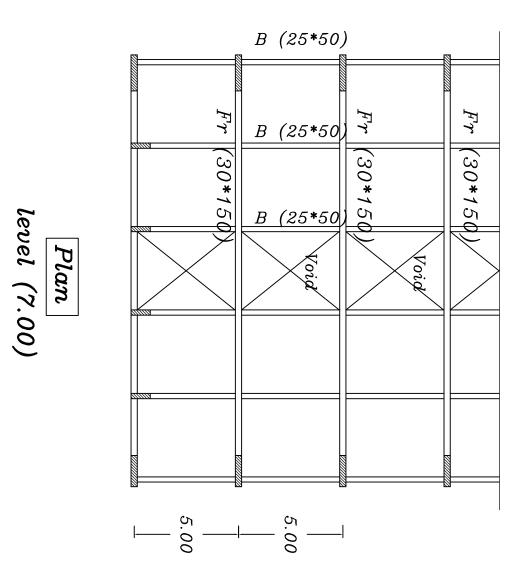




B (25\*50)

Plan

(9.00)

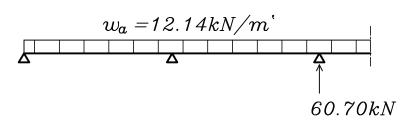




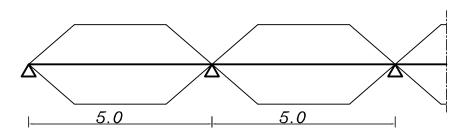
$$w_{a} = \gamma_{c}b(t-t_{s})*1.40 + C_{a} \frac{L_{s}}{2}w_{s}$$
$$= 25*0.25[0.5-0.10]*1.40 + 0.6*\frac{4}{2}*7.20$$

$$w_a = 12.14kN/m'$$

$$R_1 = 12.14*5 = 60.7kN$$



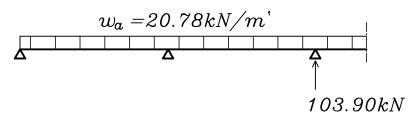
#### For $B_2$



$$w_{a} = \gamma_{c}b(t-t_{s})*1.40 + C_{a} \frac{L_{s}}{2}w_{s}*2$$
$$= 25*0.25[0.5-0.10]*1.40 + 0.6* \frac{4}{2}*7.20*2$$

$$w_a = 20.78kN/m'$$

$$R_2 = 20.78*5 = 103.9kN$$



#### For sky light

#### For $B_3$

$$w_a = 25*0.25[0.5-0.12]*1.40+0.6*\frac{4}{2}*7.90$$
  
 $w_a = 12.81kN/m$ 

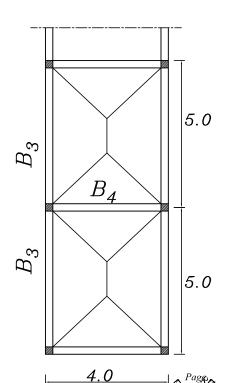
$$R_3 = 12.81*5 = 64.03kN$$

### $For B_4$

$$w_a = 25*0.25[0.5-0.12]*1.40+0.6*\frac{4}{2}*7.9*2$$
  
 $w_a = 19.13kN/m$ 

$$R_{\Delta} = 19.13*2 = 38.25kN$$

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# For Frame(1)

$$b=30cm$$

$$t = \frac{20}{12-14} = 1.5m$$

$$P_1 = 60.70kN$$
 ,  $P_2 = 103.9kN$ 

$$P_3 = R_1 + R_3 + R_4 + o.w$$
 of Post

$$=60.7+64.03+38.25+0.25*0.25*25*1.4*2$$

$$P_3 = 167.36kN$$

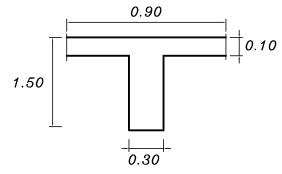
$$w_{a} = w_{e} = \%b(t - t_{s}) *1.40 + \frac{\sum A}{Span} w_{s}$$
$$= 25 *0.3[1.5 - 0.1] *1.40 + \frac{4 *2 *0.5 *8}{2.0} *7.2$$

$$w_a = w_e = 26.22 \text{ kN/m}$$

$$I_c = \frac{0.3*(\frac{5}{6}*1.5)^3}{12} = 0.049m^4$$

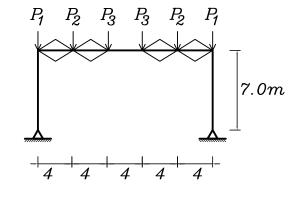
# To get $I_b$ :

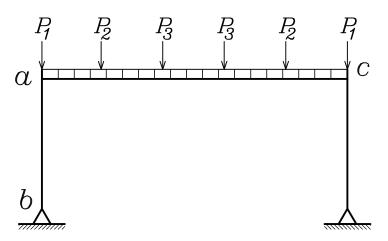
we have two cross-sections

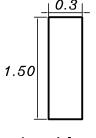


$$I_{b2} = 363*10^{-4}*0.9*1.5^{3}$$

$$I_{b2} = 0.11 m^4$$







 $at \ midspan$ 

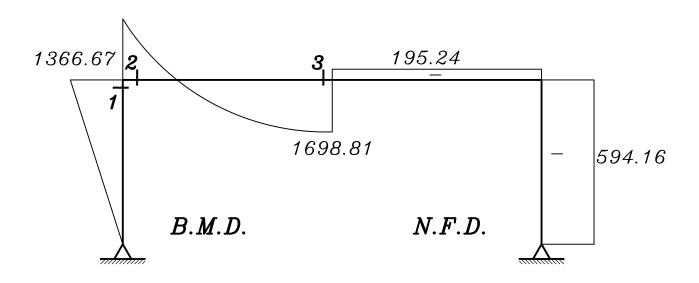
$$I_{b1} = 0.3 * \frac{1.5}{12} = 0.084 m^4$$

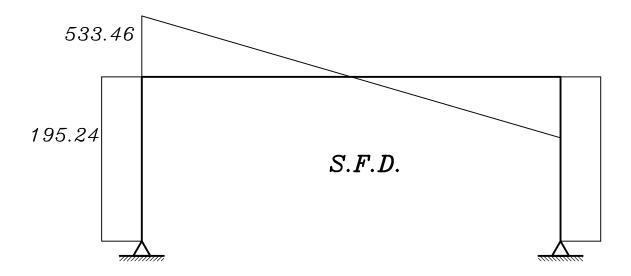
$$I_{av.} = \frac{0.11*16+0.084*4}{20} = 0.10m^4$$





$$D.f_{ab} = \frac{0.75*(0.049/7)}{0.75(\frac{0.049}{7})+0.5(\frac{0.11}{20})} = 0.68$$







#### Sec(1-1)

$$\frac{N_u}{bt f_{cu}} = \frac{594.16*10^3}{300*1500*25} = 0.053>0.04(Don't neglect N)$$

$$e = \frac{M}{N} = \frac{1366.67}{594.16} = 2.3m$$

$$\frac{e}{t} = \frac{2.3}{1.5} = 1.5 > 0.5$$
 (big eccentricity)

$$e_s = e + \frac{t}{2} - c = 2.3 + \frac{1.5}{2} - 0.1 = 2.95m$$

$$M_{us} = N * e_s = 594.16 * 2.95 = 1752.87 kN.m$$

$$1400 = C_1 \sqrt{\frac{1752.87*10^6}{300*25}} C_1 = 2.90 \quad J = 0.73$$

$$A_{s} = \frac{1752.87*10^{6}}{0.73*1400*360} - \frac{594.16*10^{3}}{(360/1.15)} = 28.58cm^{2}$$

8ø22

#### Sec. (2-2)

$$\frac{N}{bt f_{cu}} = \frac{195.24*10^3}{300*1500*25} = 0.017 < 0.04 \ (neglect \ N)$$

$$1400 = C_1 \sqrt{\frac{1366.67*10^6}{300*25}} \qquad C_1 = 3.28 \qquad J = 0.77$$

$$A_{s} = \frac{1366.67*10^{6}}{0.77*1400*360} = 35.37cm^{2}$$

10ø22

### Sec. (3-3)

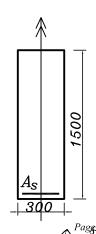
$$R-Sec$$
  $b=300mm$ ,  $d=1400mm$ 

$$d = 1400 mm$$

, 
$$M_{ul}$$
 =1698.81 $k$ N. $m$ ,  $N_{u.l.}$  (neglected)

$$R-Sec)$$
 هو  $Sec(3-3)$  صريح

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$$1400 = C_1 \sqrt{\frac{1698.81*10^6}{300*25}} \qquad C_1 = 2.94 \qquad J = 0.74$$

$$A_s = \frac{1698.81*10^6}{0.74*1400*360} = 45.76 \text{ cm}^2$$

10ø25

#### Check Shear

$$Q_{cr} = Q_{max} - w(\frac{c}{2} + \frac{d}{2})$$

$$Q_{cr} = 533 - 26.2(\frac{1.50}{2} + \frac{1.40}{2})$$

$$Q_{cr} = 495 \text{ kN}$$

$$q_{su} = \frac{Q_{cr}}{bd} = \frac{495*10^{3}}{300*1400} = 1.18 \text{ N/mm}^{2}$$

$$q_{cu} = 0.24\sqrt{\frac{25}{1.5}} = 0.98 \text{ N/mm}^{2}$$

 $q_{cu} < q_u < q_{umax}$ 

$$q_{max} = 0.7 \sqrt{\frac{25}{1.5}} = 2.86 \ N/mm^2$$

$$q_u - \frac{q_{cu}}{2} = \frac{nA_s f_y / \gamma_s}{bS}$$

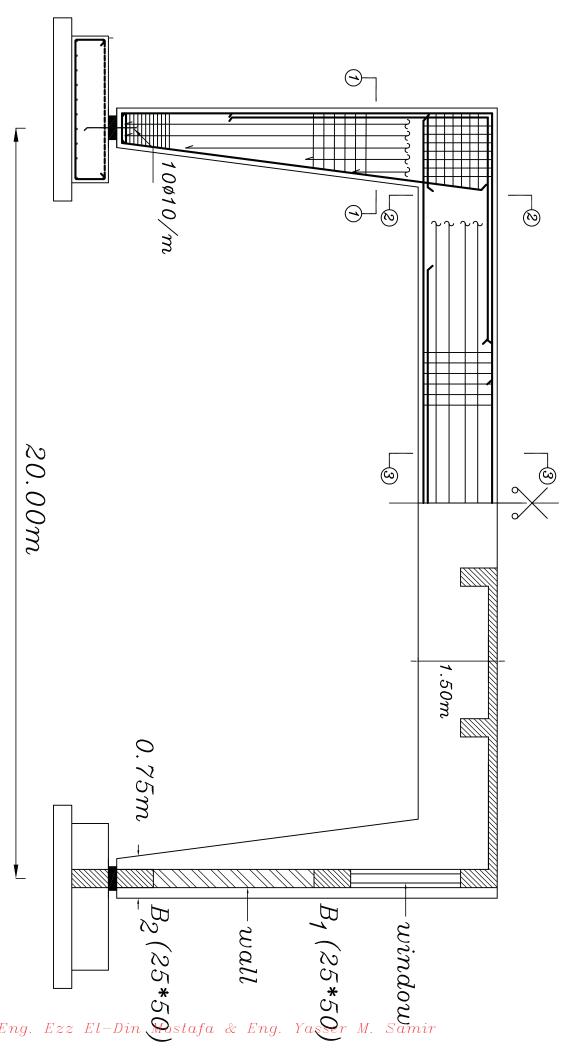
assume n=2

$$A_{s} = 78.5 mm^{2} = \emptyset10$$

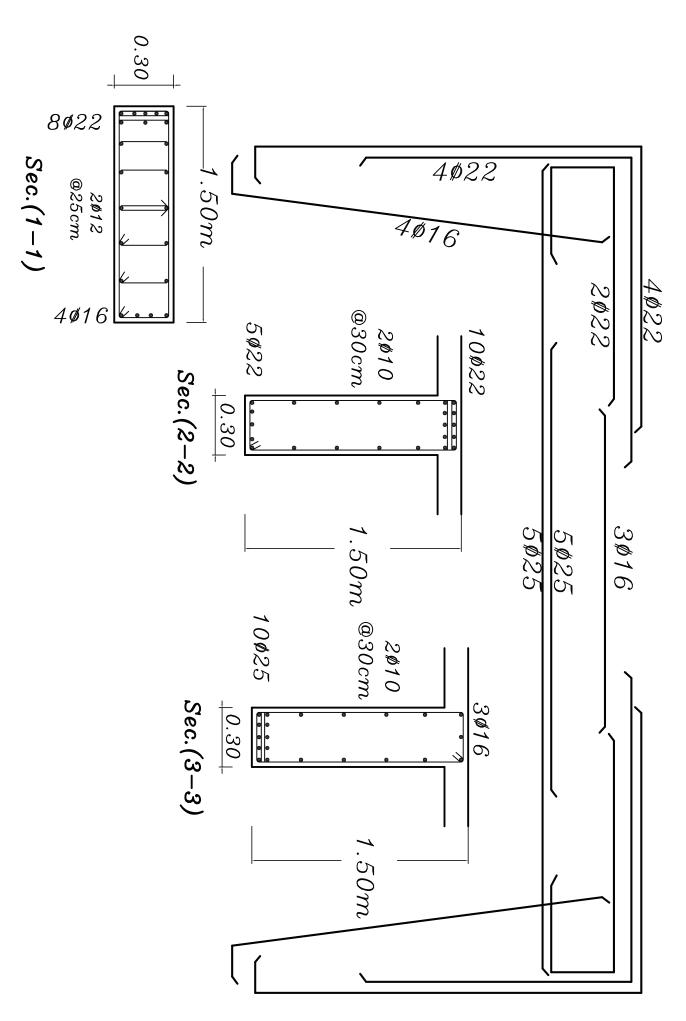
$$1.18 - \frac{0.98}{2} = \frac{2*78.5*240/1.15}{300*S} \implies S=158mm$$

No. of 
$$stirrups/m' = \frac{1000}{S} = 6.3$$
 Take Stirrups 7010/m'











For the given plan and cross-section, it is required to:

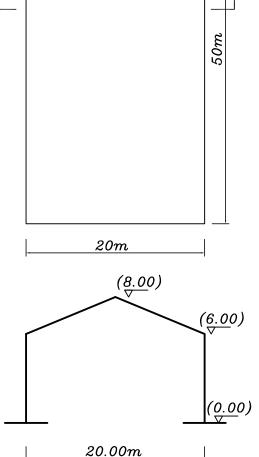
1 - Draw structural plan and cross section to show all concrete elements.

2- Design the slabs and Main supporting element.

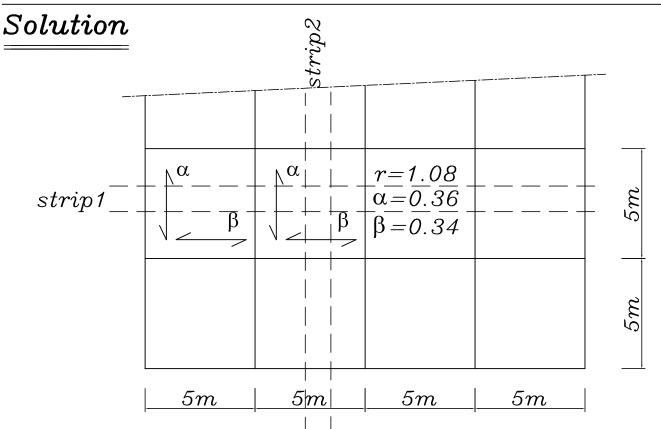
given Use Sec. Beams 25\*50

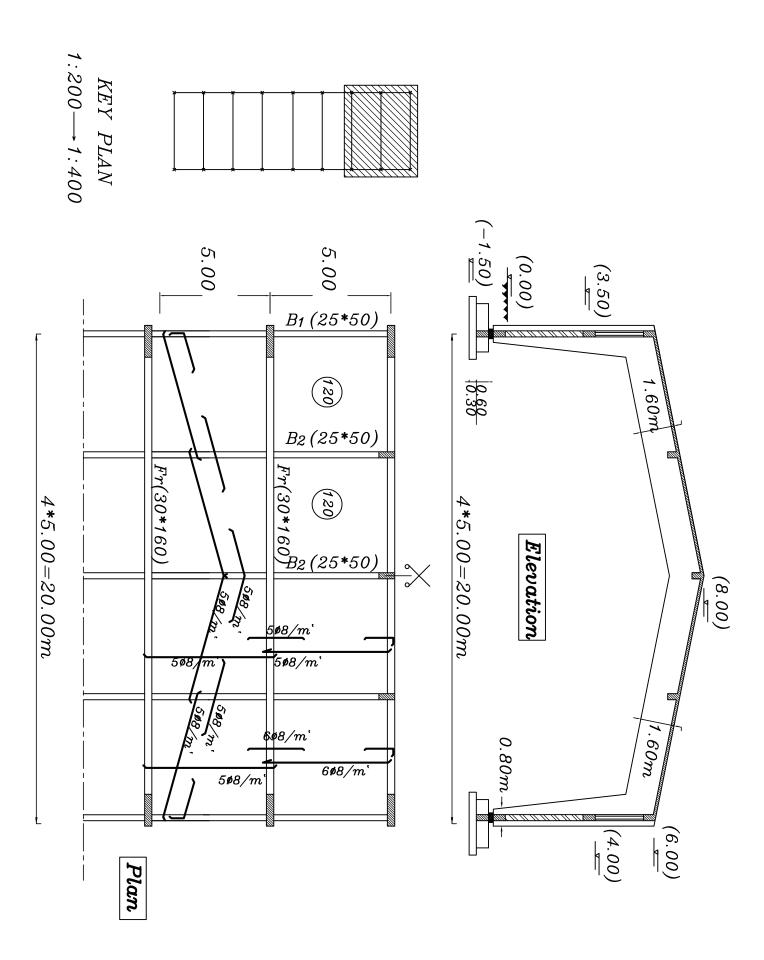
$$f_{cu}$$
=25 $N/mm^2$   $f_y$ =360 $N/mm^2$ 

$$F. C. = 1.5kN/m^2$$
  $L. L. = 1.0kN/m^2$ 



Sec.(1-1)







## 1- Design of slabs

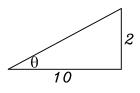
$$t_{s} = \frac{500}{45} = 11.11 cm$$

Take  $t_s = 12cm$  For all slabs

$$w_{su} = 1.4[t_s \gamma_c + F.c.] + 1.6 L.L.Cos\theta$$

$$w_{su} = 1.4[0.12*25+1.5]+1.6*1.0*0.98$$

$$w_{su} = 7.87 \ kN/m^2$$



$$\theta = tan^{-1}(\frac{2}{10})$$

$$\theta = 11.31$$

$$\cos \theta = 0.98$$

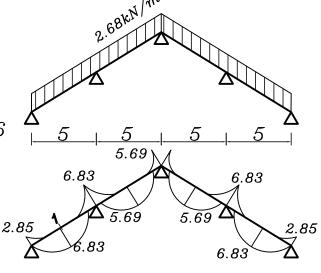
## Strip(1)

Sec. 
$$(1-1)$$
  $d=120-30=90 \text{ mm}$ 

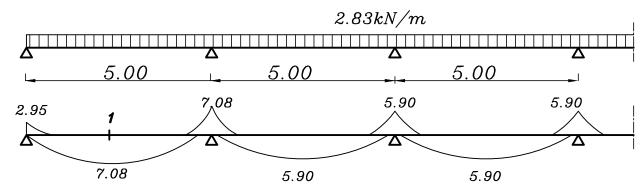
$$90 = C_1 \sqrt{\frac{6.83*10^6}{1000*25}} \quad C_1 = 5.44 \quad J = 0.826$$

$$A_{s} = \frac{6.83*10^{6}}{0.826*360*90} = 255 \text{mm}^{2} / \text{m}'$$

$$A_s = 5 \oplus 8/m$$



## Strip(2)



**Sec.** 
$$(1-1)$$
  $d=120-20=100 \text{ mm}$ 

$$100 = C_{1} \sqrt{\frac{7.08 * 10^{6}}{1000 * 25}} \quad C_{1} = 5.3 \qquad J = 0.826$$

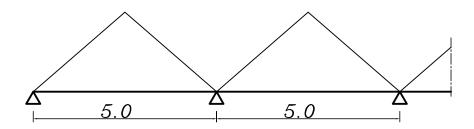
$$A_{\rm s} = \frac{7.08*10^6}{0.826*360*100} = 238 \text{mm}^2 / \text{m}'$$

 $A_s = 5 \# 8^{E} m^{Ezz}$  El-Din Mostafa & Eng. Yasser M. Samir



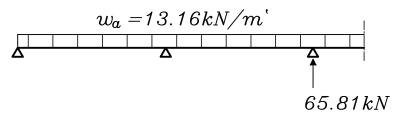
### 2-Analysis of Beams

#### For $B_1$

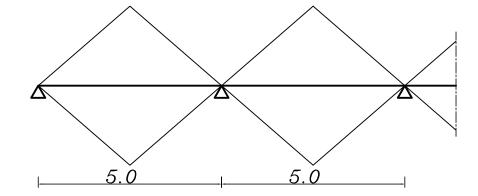


Assume beams (25\*50)

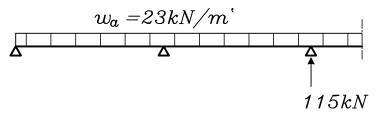
$$w_a = \gamma_c b(t - t_s) * 1.40 + C_a \frac{L_s}{2} w_s$$
  
=  $25 * 0.25 [0.5 - 0.12] * 1.40 + 0.5 * \frac{5}{2} * 7.87$   
 $w_a = 13.16 kN/m$ 



### For $B_2$

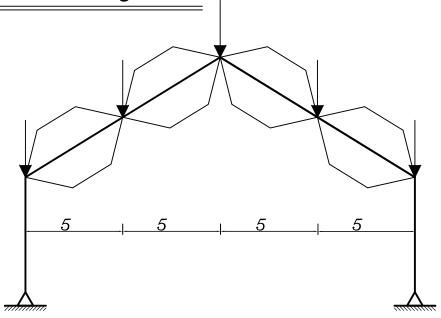


$$w_a = \gamma_c b(t - t_s) *1.40 + C_a \frac{L_s}{2} w_s *2$$
  
=  $25 *0.25[0.5 - 0.12] *1.40 + 0.5 * \frac{5}{2} *7.87 *2$   
 $w_a = 23kN/m$ 





### 3-Analysis of Main system

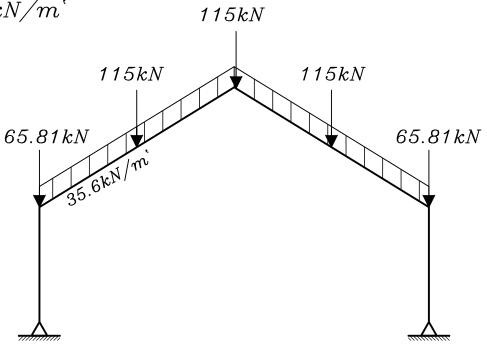


assume b=30cm ,  $t=\frac{L}{12-14}=\frac{20}{12-14}=1.6m$ 

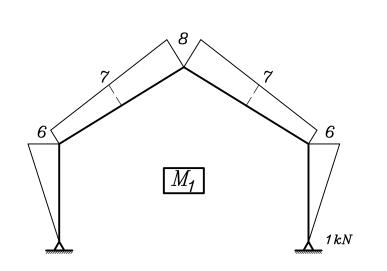
 $Load\ For\ Shear\ = Load\ for\ Moment$ 

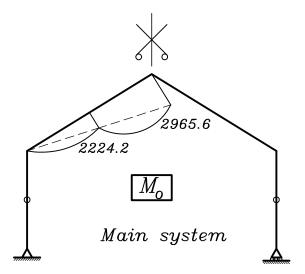
$$w_{a} = w_{e} = \% \ b(t - t_{s}) * 1.40 + \frac{\sum A}{Span} \ w_{s}$$
$$= 25 * 0.3[1.6 - 0.12] * 1.40 + \frac{6.50 * 8}{20.4} * 7.87$$

$$w_a = w_e = 35.6kN/m$$



we have to use virtual work method in this example, because if we use moment distribution, we have to make sway correction.





$$\delta_{10} = \frac{M_0 M_1}{EI}$$

$$\delta_{11} = \frac{M_1^2}{EI}$$

$$I_c = \frac{0.3*(\frac{5}{6}*1.6)^3}{12} = 0.059m^4$$

$$I_b = \mu B t^{3} * 10^{-4}$$

$$=341*1.02*1.6^{3}*10^{-4}=0.143m^{4}$$

$$\begin{array}{c|c}
B = 6t_s + b = 1.02m \\
\hline
1.60 \\
\hline
0.30
\end{array}$$

$$\frac{t_s}{t} = \frac{0.12}{1.60} = 0.075$$

$$\frac{b_0}{B} = \frac{0.3}{1.02} = 0.29$$

$$\delta_{10} = -\frac{1}{3} * \frac{5.10}{E_c} [2224.2*7 + 2224.2* \frac{6}{2}] *2$$

$$-\frac{1}{3} * \frac{5.10}{E_c} [2224.2*7 + 2965.6*8 + \frac{2224.2*8}{2} + \frac{2965.6*7}{2}] * 2$$

$$-\frac{2}{3} * \underbrace{\frac{5.10}{E_c I_b}} [\underbrace{\frac{35.6*5.1*5}{8}} * 6.50] * 2 - \frac{2}{3} * \underbrace{\frac{5.10}{E_c I_b}} [\underbrace{\frac{35.6*5.1*5}{8}} 7.5] * 2$$

$$\delta_{10} = \frac{-1996962.567}{E_c}$$

$$\delta_{11} = \frac{1}{3} * \frac{6}{E_c I_b} [6*6]*2 + \frac{1}{3} * \frac{10.2}{E_c I_b} [6^2 + 8^2 + 6*8]*2$$

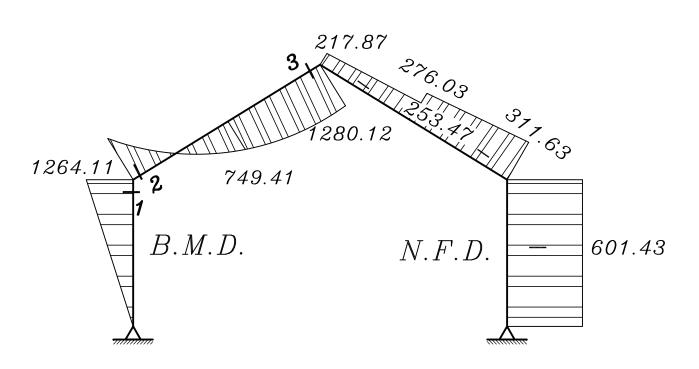
$$\delta_{11} = rac{9478.44}{E_{
m C}}_{By~Eng.~Ezz~El-Din~Mostafa~\&~Eng.~Yasser~M.~Samir}$$

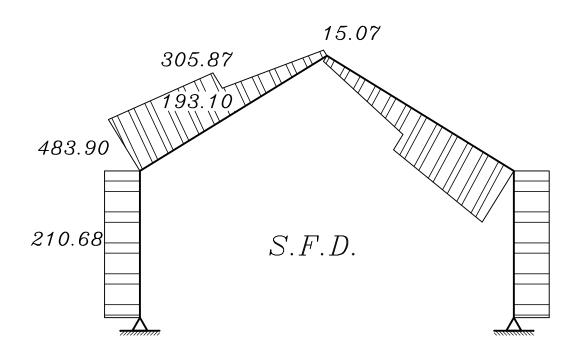


$$\delta_{10}+ x \delta_{11}=0$$

$$-\frac{1996962.567}{E_c} + \frac{9478.44}{E_c} X=0$$

$$X=210.68kN$$







### Sec(1-1)

$$\frac{N_{u.l.}}{b\ t\ f_{cu}} = \frac{601.43*10^3}{300*1600*25} = 0.05 > 0.04 (Don't\ neglect)$$

$$e = \frac{M_{u.l.}}{N_{u.l.}} = \frac{1264.11}{601.43} = 2.10m$$

$$\frac{e}{t} = \frac{2.1}{1.6} = 1.3 > 0.5 (big\ eccentricity)$$

$$e_s = e + \frac{t}{2} - c = 2.1 + \frac{1.6}{2} - 0.1 = 2.80m$$

$$M_{us} = N_{u.l.} e_s = 601.43 * 2.80 = 1685.11 kN.m$$

$$1500 = C_1 \sqrt{\frac{1685.11*10^6}{300*25}} \quad C_1 = 3.16 \quad J = 0.76$$

$$A_{s} = \frac{1685.11*10^{6}}{0.76*1500*360} - \frac{601.43*10^{3}}{360/1.15} = 21.96cm^{2}$$

6ø22

# Sec. (2-2)

$$\frac{N_{u.l.}}{b\ t\ f_{cu}} = \frac{311.63*10^3}{300*1600*25} = 0.02 < 0.04\ (neglect\ N)$$

$$1500 = C_1 \sqrt{\frac{1264.11*10^6}{300*25}}$$
  $C_1 = 3.65$   $J = 0.79$ 

$$A_{s} = \frac{1264.11*10^{6}}{0.79*1500*360} = 29.67cm^{2}$$

8ø22



## Sec(3-3)

$$N_{u,l} = 217.87kN$$
 (neglect N)

$$M_{u,l} = 1280.12kN.m$$

$$B = \begin{bmatrix} 16*120+300=2220\\ -5000\\ \frac{0.76*20.4*1000}{5} +300=3400 \end{bmatrix}$$

B = 2220mm

$$1500 = C_1 \sqrt{\frac{1220.12*10^6}{2220*25}} \qquad C_1 = 9.88 \qquad J = 0.826$$

$$A_{\rm s} = \frac{1280.12*10^6}{0.826*1500*360} = 28.70cm^2$$

8022

#### Check Shear

$$Q_{cr} = Q_{max} - w \left[ \frac{C}{2} + \frac{d}{2} \right] Cos \theta$$

$$Q_{cr} = 483.93 - 35.6 \left[ \frac{1.60}{2} + \frac{1.50}{2} \right] Cos \theta$$

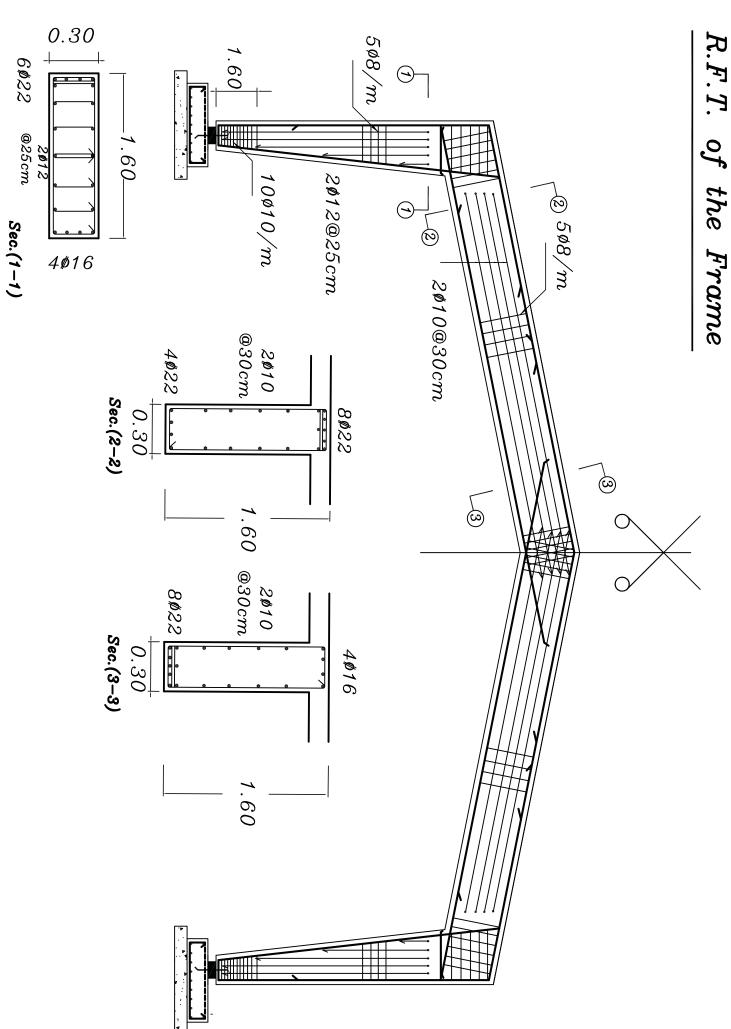
$$Q_w = 429.79kN$$

$$q_{su} = \frac{Q_{cr}}{bd} = \frac{429.79*10}{300*1500}^3 = 0.96N/mm^2$$

$$q_{cu} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 N/mm^2$$

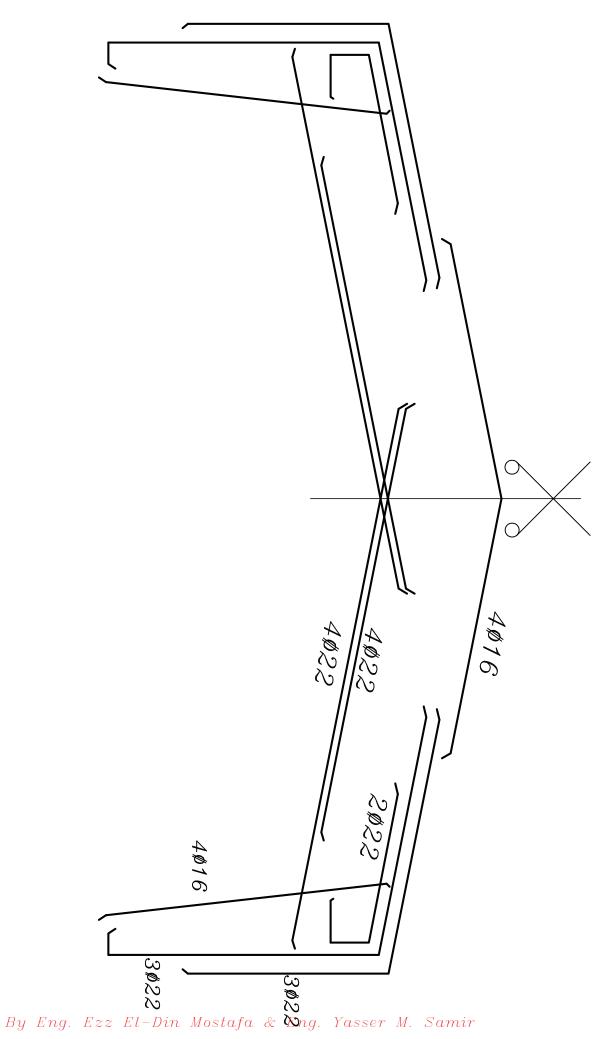
$$q_{su} < q_{cu}$$
 508/m°







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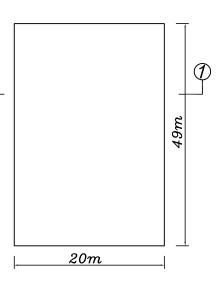


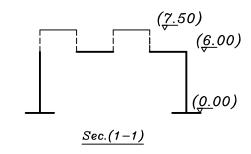


For the given plan and cross- section,

#### it is required to:

- 1- Draw structural plan and cross section to show all concrete elements.
- 2- Show how to solve the main system





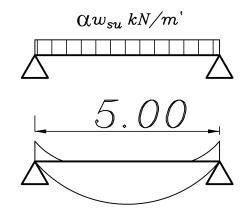
## Solution

#### 1-Design for solid slabs:

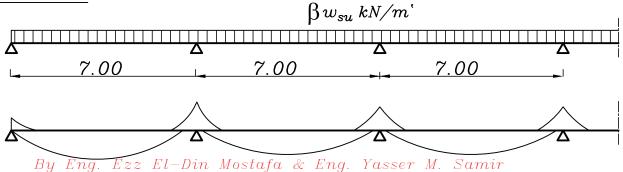
$$t_{\rm S} = \frac{L_{\rm S}}{20} = \frac{500}{35} = 14.2cm$$

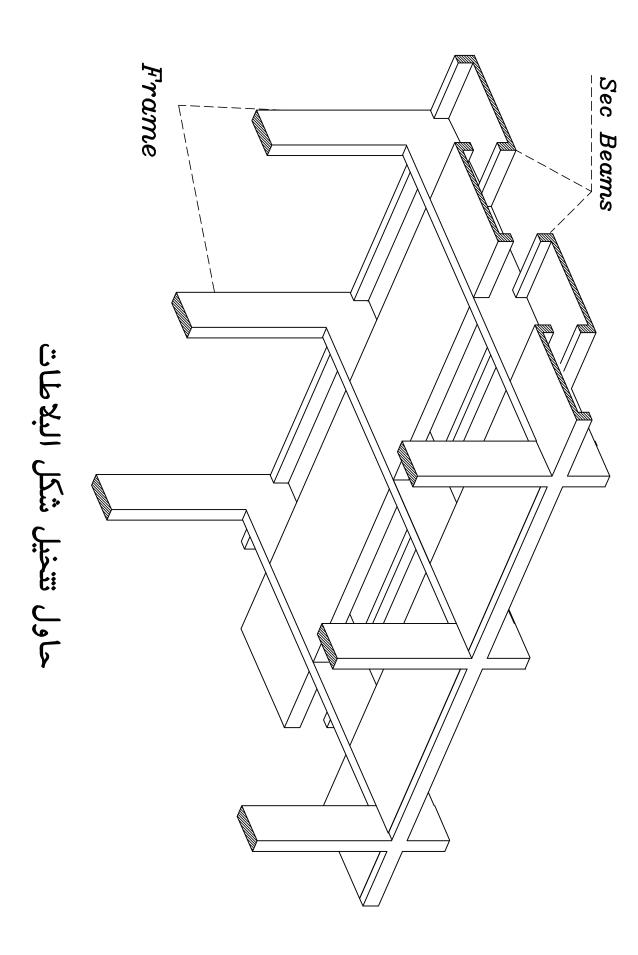
take  $t_s = 15cm$  for all slabs (check deflection)

# Strip(1)

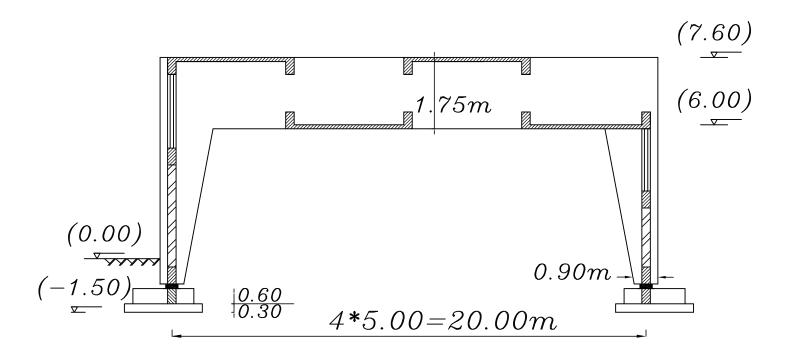


### Strip(2)

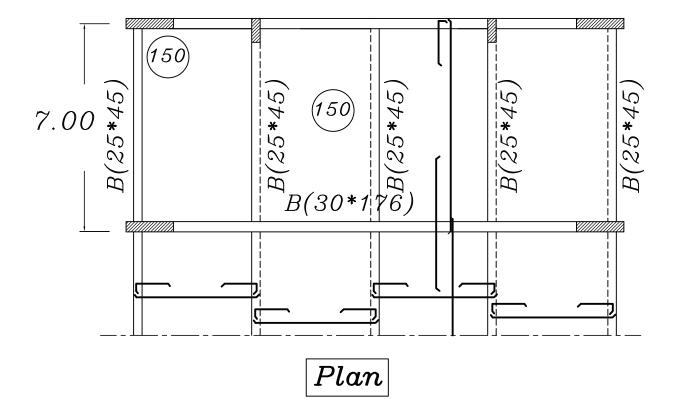








# ${\it Elevation}$



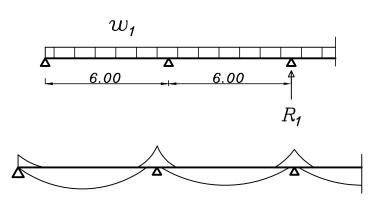


#### 2- Design for secondary beams

### For $B_1$

$$w_1 = \gamma_c b(t - t_s) * 1.4 + w_s \frac{L_s}{2}$$

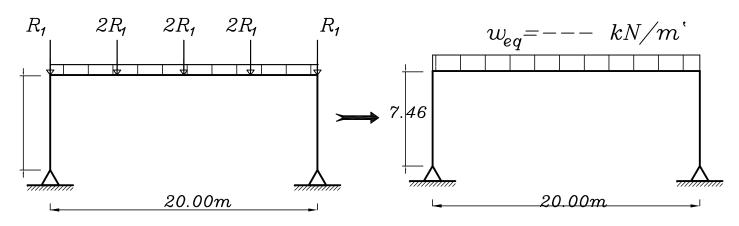
$$R_1 = w_1 * Spacing$$

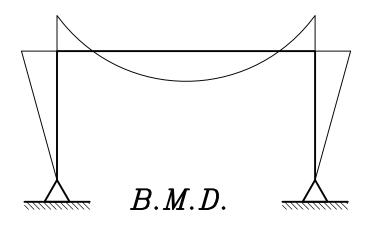


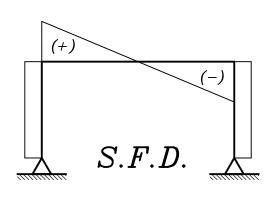
#### 3-Design of Main System

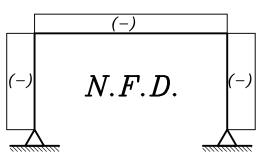
assume 
$$b=30cm$$
 ,  $t=\frac{L}{12-14}=\frac{18}{12-14}=1.40m$ 

$$w_{eq} = o.w + \frac{\sum P}{L}$$







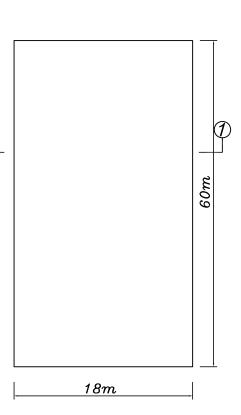


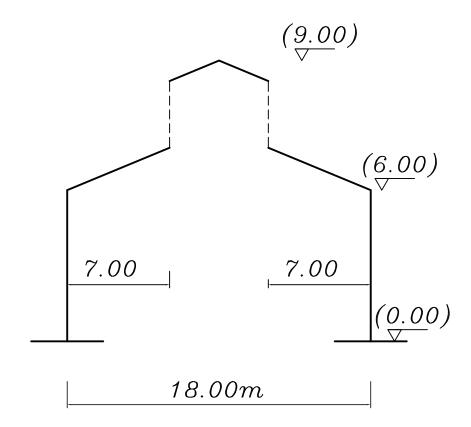
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For the given plan and cross-section, it is required to:

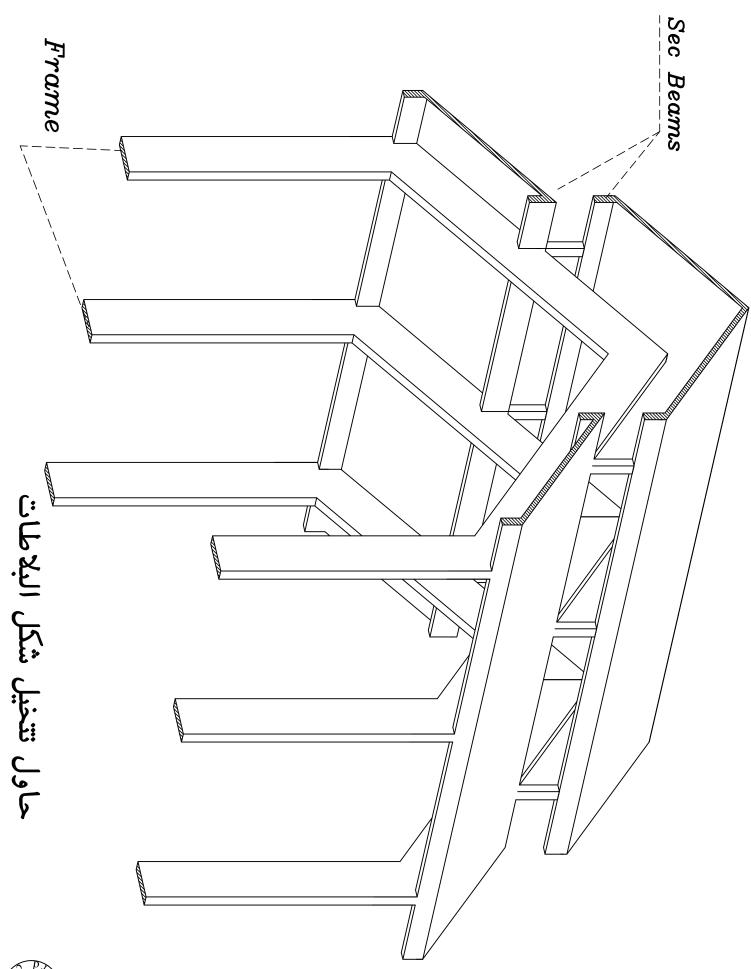
Draw structural plan and cross section to show all concrete elements.





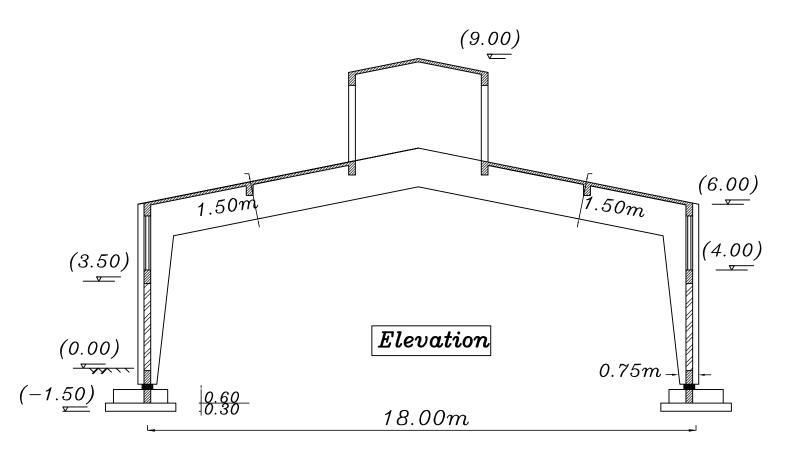
$$Sec.(1-1)$$

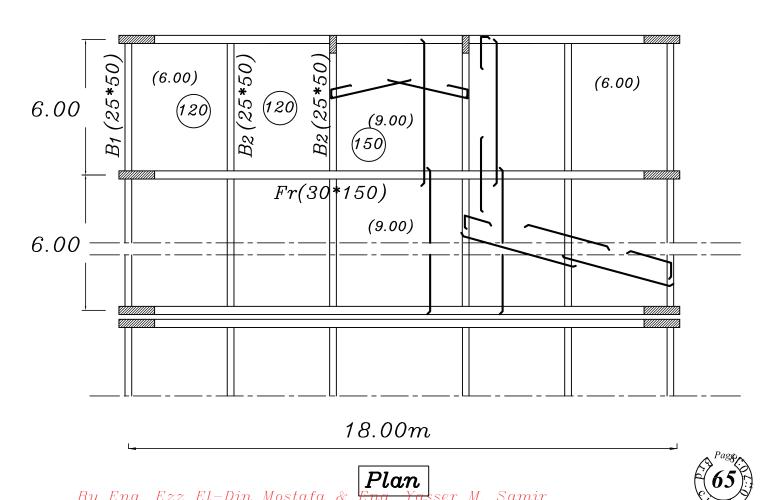






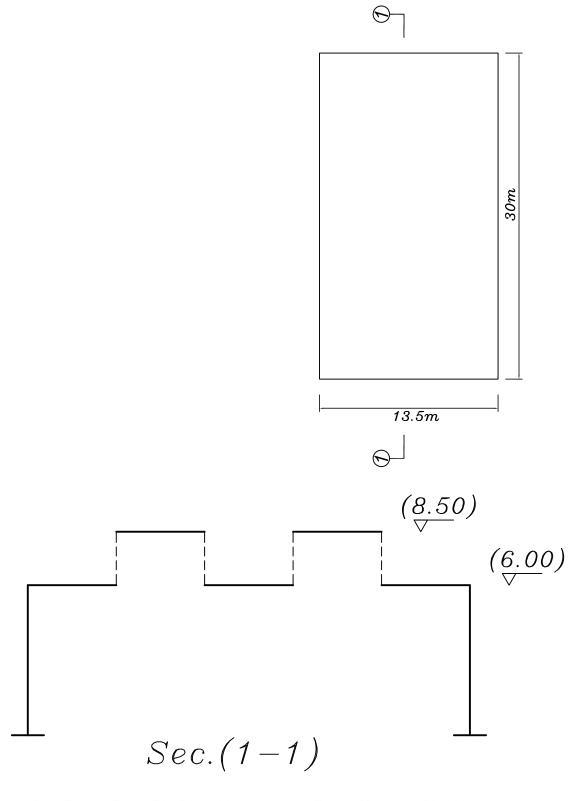
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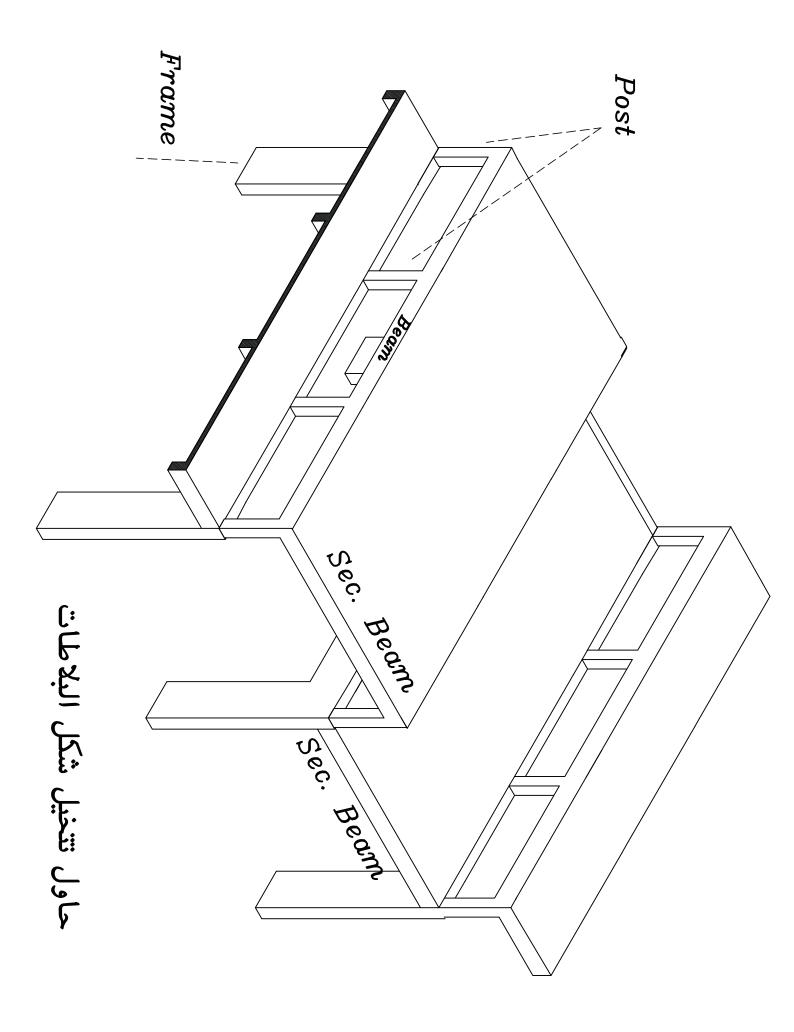
For the given plan and cross- section, it is required to:

Draw structural plan and cross section to show all concrete elements.



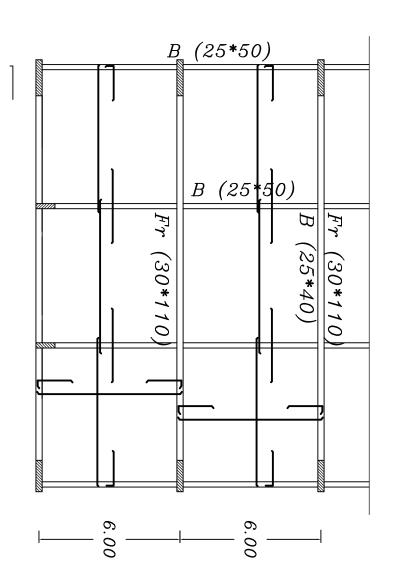
Paggo

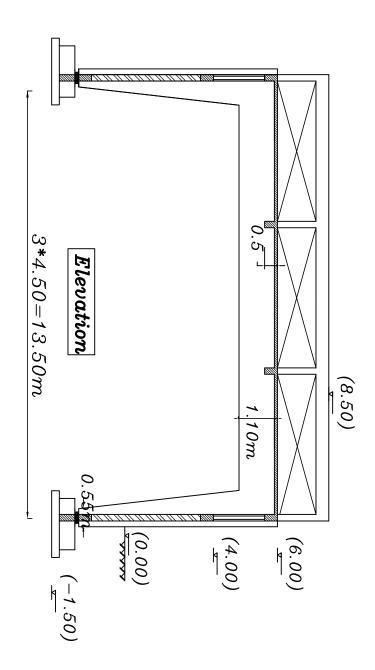
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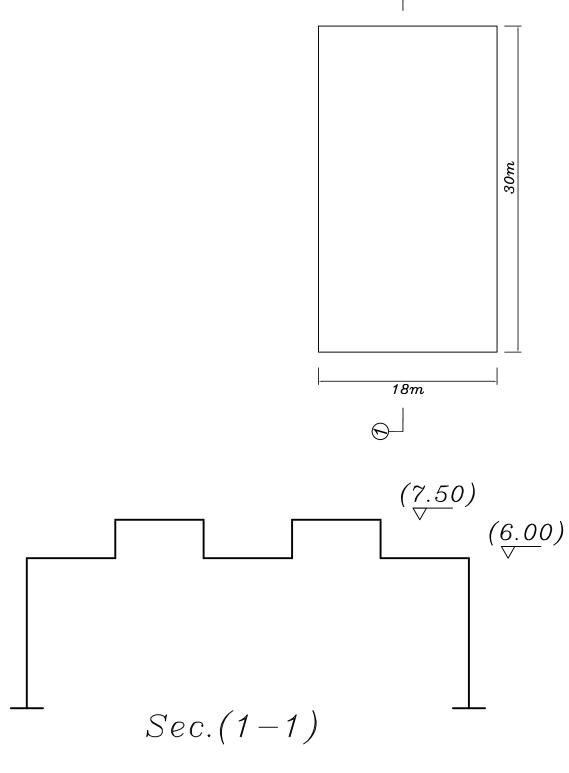
Plan





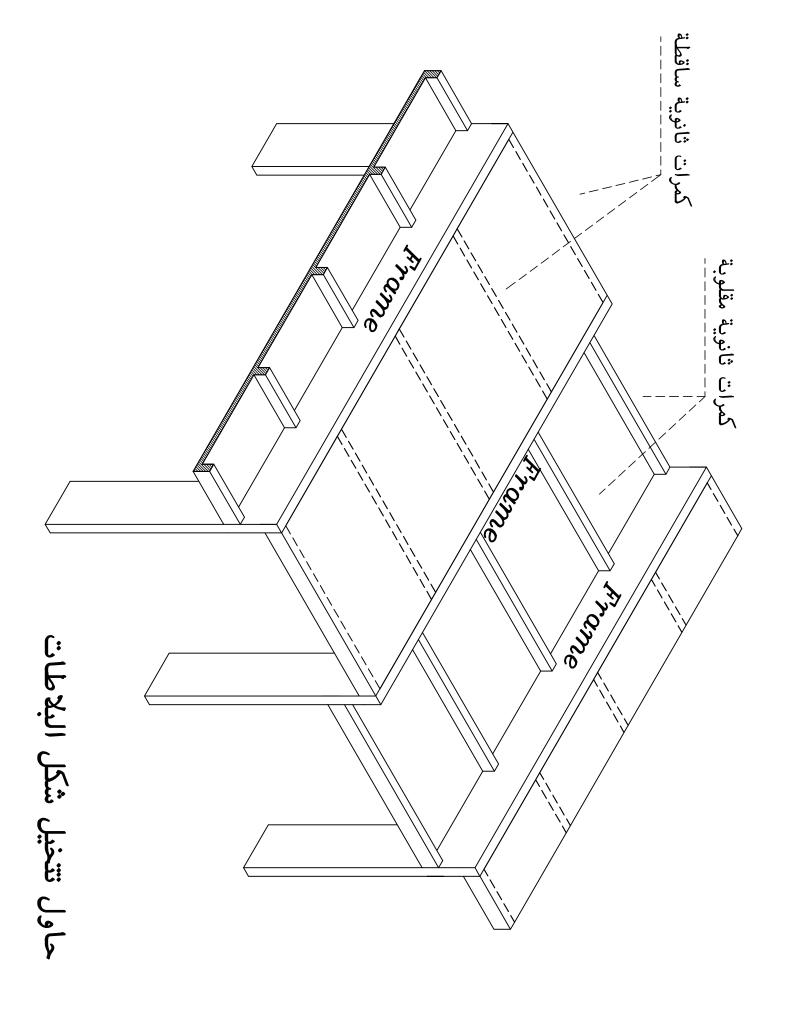
For the given plan and cross- section, it is required to:

Draw structural plan and cross section to show all concrete elements.

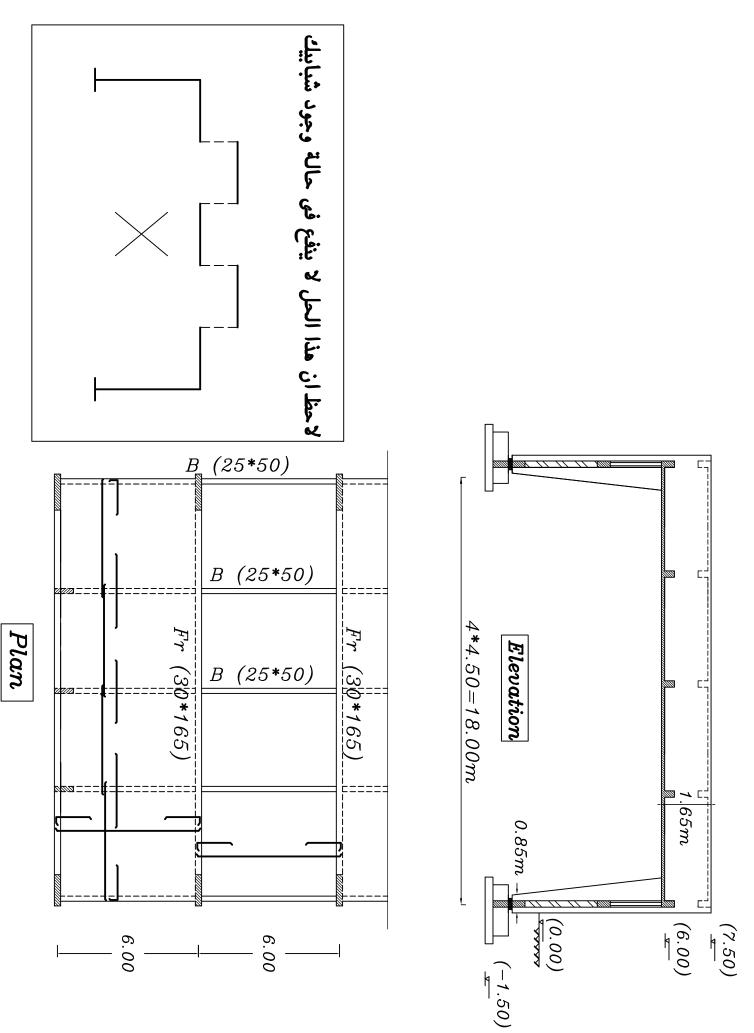


Paggo

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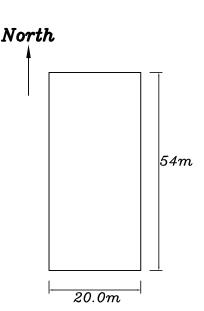
### Saw Tooth Supported on a system

اذا كانت المسافة بين الاعمدة اكبر من ١٢ م فاننا نختار احد الانظمة الانشائية مثل وذلك حسب الطول القصير للارض واتجاه (Saw tooth)

#### Example

For the given plan, it is required to:

- 1-Choose the suitable system to cover this Area.
- 2-Design all Slabs and draw plan of Rft.
- 3-Design the main supporting element and draw details of Rft.



$$F.C. = 1.5kN/m^2$$
 ,  $L.L = 0.5 kN/m^2$ 

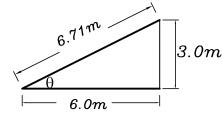
$$f_{cu} = 25 \ N/mm^2$$
,  $f_y = 360 \ N/mm^2$ 

Columns are only allowed on perimeter

#### Solution

$$t = \frac{671}{16} = 41.94cm$$

$$take \ t=25 \ cm \ [20cm+5cm]$$



$$\theta = tan^{-1}(\frac{3}{6.0}) = 26.57$$

$$w_{su} = 1.4(t_s \gamma_c + F.C. + 2bh \gamma_c + 10*wt.of block] + 1.6L.L.Cos \theta$$

$$w_{su}=1.4(0.05*25+1.5+2*0.1*0.2*25+10*0.15]+1.6*0.5*0.89$$

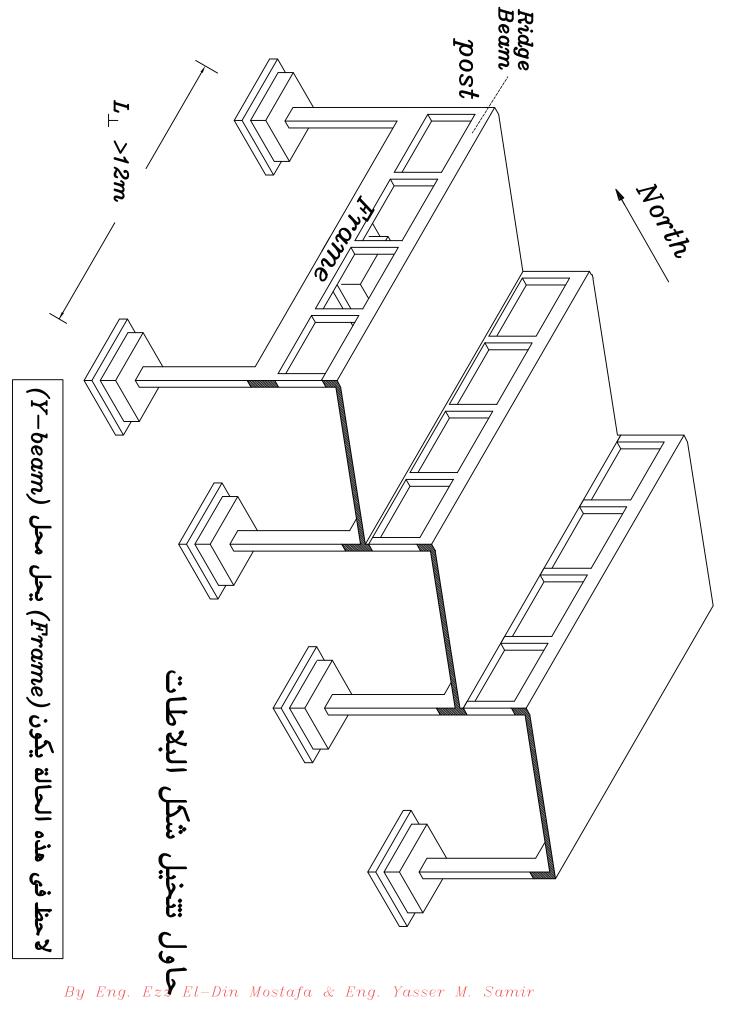
$$w_{su}=8.06kN/m^2$$

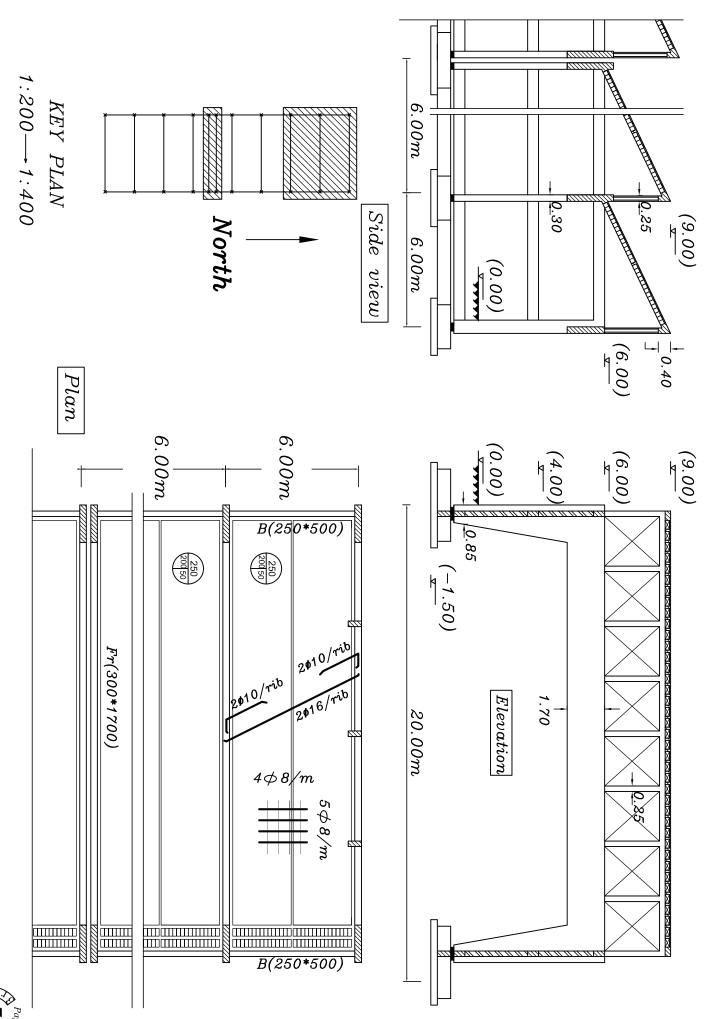
$$w_{su/Rib} = 0.5*8.06 = 4.03kN/m$$

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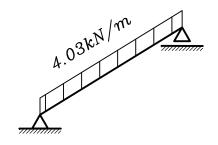








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Sec. (1-1)

$$220 = C_1 \sqrt{\frac{20.28*10^6}{500*25}}$$

$$C_1 = 5.46$$
  $J = 0.826$ 

$$A_{\rm S} = \frac{20.28*10^6}{0.826*360*220} = 3.10 \, {\rm cm}^2/{\rm rib}$$

$$A_s = 2 \oplus 16/rib$$

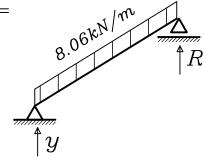
Sec. 
$$(2-2)$$

$$A_s = 2 \oplus 10/rib$$

## 2]Reactions of slabs on beams

$$R=y=w_{su}\frac{L}{2}$$
  $kN/m$ 

$$R=y=8.06*6.71/2=27.04 \ kN/m$$

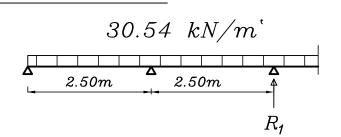


# 3]Analysis of Ridge beam(250\*400)

$$w=R+o.w$$
  $kN/m$   
 $w=27.04+0.25*0.40*25*1.40$ 

$$w = 30.54 \ kN/m$$

$$R_1 = 30.54*2.5 = 76.35kN$$



# 4]Design of Posts

$$R_p = R_1 + o.w$$
 of  $Post$ 

$$R_{p} = 76.35 + 0.25*0.25*3*25*1.40 = 82.91kN$$

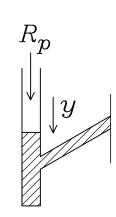
$$82.91*10^{3} = 0.35*250*250*25 + 0.67A_{s} f_{y}$$

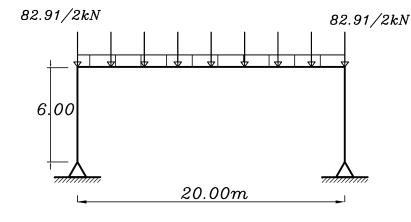
$$A_{s} = -ve \longrightarrow A_{s} = 4013$$

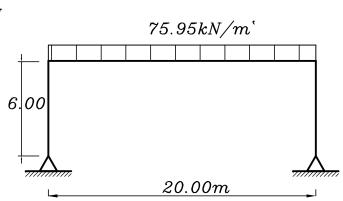
## 5]Design of main system

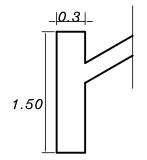
## (Y-beam) هو نفسه (Frame) لاحظ في هذه الحالة يكون

$$w_f = 0.w. + y + \frac{\Sigma R_p}{Span}$$
  $kN/m$   $w_f = 0.30*1.50*25*1.40+27.04+ \frac{8*82.91}{20.0}$   $w_f = 75.95kN/m$ 









$$I_b = 0.3 * \frac{1.5}{12} = 0.084 m^4$$

$$I_{c} = \frac{0.30*(\frac{5}{6}*1.50)}{0.3}$$

$$I_{c} = \frac{0.30*(\frac{5}{6}*1.50)^{3}}{12}$$

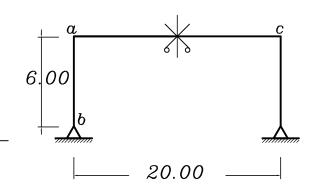
$$I_{c} = 0.049m^{4}$$



#### For Joint a

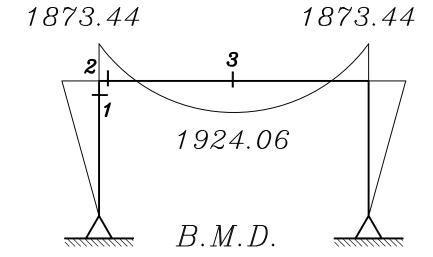
$$D.f_{ab} = \frac{0.75(I_c/h)}{(0.75\frac{I_c}{h}) + (0.5\frac{I_b}{L})}$$

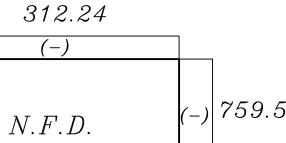
$$D.f_{ab} = \frac{0.75*(0.049/6.00)}{0.75*(0.049/6.00)+0.50*(0.084/20)}$$

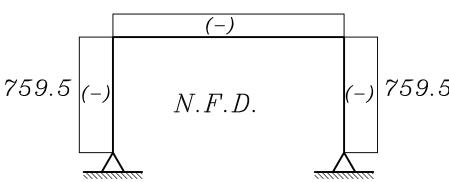


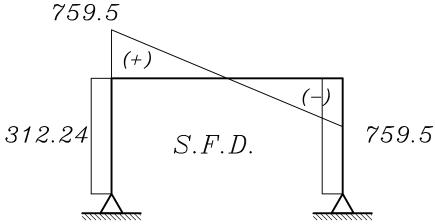
$$D.f_{ab} = 0.74$$
  $D.f_{ac} = 1 - 0.74 = 0.26$ 

$$F.E.M. = 75.95*20^{2}/12 = 2532 \ kN$$









By Eng. Ezz El-Din Mostafa & Eng. Yasser M. Samir



#### Design of Sections

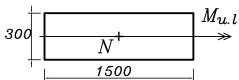
Sec. 
$$(1-1)$$

Sec. 
$$(1-1)$$
  $M_{u,h} = 1873.44kN.m$ 

 $N_{u,l} = 759.50kN.m$ 

$$b=300mm$$
 ,  $t=1500mm$ 

$$t = 1500 mm$$



$$\frac{N_{u.l.}}{btf_{cu}} = \frac{759.50*10^{3}}{300*1500*25} = 0.068>0.04 \text{ (Dont neglect } N_{u.l.} \text{)}$$

$$e = \frac{M_{u.l.}}{N_{u.l.}} = \frac{1873.44}{759.50} = 2.47m$$

$$\frac{e}{t} = \frac{2.47}{1.50} = 1.64 > 0.5$$
 (big eccentricity)

$$e_s = e + \frac{t}{2} - c = 2.47 + \frac{1.50}{2} - 0.1 = 3.12m$$

$$M_{us} = 759.50*3.12 = 2367.12kN.m$$

$$d = C_1 \sqrt{\frac{Mus}{b * f_{cu}}}$$

$$1400 = C_1 \sqrt{\frac{2367.12*10^6}{300*25}}$$
  $C_1 = 2.49 < 2.78$   $take \ d = 1600mm$ 

$$e_s = e + \frac{t}{2} - c = 2.47 + \frac{1.70}{2} - 0.1 = 3.22m$$

$$M_{us} = 759.50*3.22 = 2445.59kN.m$$

$$1600 = C_1 \sqrt{\frac{2445.59*10^6}{300*25}} \qquad C_1 = 2.80 \& J = 0.72$$

$$A_{\rm S} = \frac{{\it Mus}}{{\it J.d.f_y}} \ - \frac{{\it Nus}}{{\it f_y}/\gamma_{\rm S}}$$

$$A_{s} = \frac{2445.59*10^{6}}{0.72*1600*360} - \frac{759.50*10^{3}}{360/1.15}$$

$$A_s = 34.75 cm^2 = 10022$$



Sec. 
$$(2-2)$$

Sec. (2-2)  $M_{u.l.} = 1873.44kN.m$ 

 $N_{u,l} = 312.24kN.m$ 

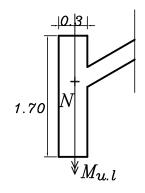
b=300mm, t=1700mm

$$\frac{N_{u.l.}}{btf_{cu}} = \frac{312.24*10^3}{300*1700*25} = 0.024<0.04 \ (neglect \ N_{u.l.})$$

$$d = C_1 \sqrt{\frac{Mu.l.}{b * f_{cu}}}$$

$$1600 = C_1 \sqrt{\frac{1873.44*10^6}{300*25}} \qquad C_1 = 3.20 \& J = 0.76$$

$$C_1 = 3.20 \& J = 0.76$$



$$A_{s} = \frac{1873.44*10^{6}}{0.76*1600*360}$$

$$A_s = 42.75 cm^2 = 12022$$

Sec. 
$$(3-3)$$
  $M_{u,h} = 1924.06kN.m$ 

 $N_{u,l} = 312.24kN.m$ 

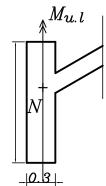
b=300mm , t=1700mm

$$\frac{N_{u.l.}}{btf_{cu}} = \frac{312.24*10^3}{300*1700*25} = 0.024 < 0.04 \ (neglect N_{u.l.})$$

$$d = C_1 \sqrt{\frac{Mu.l.}{b*f_{cu}}}$$

$$1600 = C_1 \sqrt{\frac{1924.06*10^6}{300*25}}$$
  $C_1 = 3.16 \& J = 0.76$ 

$$C_1 = 3.16 \& J = 0.76$$



$$A_{s} = \frac{1924.06*10^{6}}{0.76*1600*360}$$

$$A_s = 44.11 \, \text{cm}^2 = 12022$$

#### Check Shear

$$Q_{cr} = Q_{max} - w(\frac{c}{2} + \frac{d}{2})$$

$$Q_{cr} = 759.5 - 75.95(\frac{1.70}{2} + \frac{1.60}{2})$$

$$Q_{cr} = 634.18kN$$

$$q_{su} = \frac{Q_{cr}}{bd} = \frac{634.18*10^3}{300*1600} = 1.32 \text{ N/mm}^2$$

$$q_{cu} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 \ N/mm^2$$

$$q_{max} = 0.7 \sqrt{\frac{25}{1.5}} = 2.86 \text{ N/mm}^2$$
 $q_{cu} < q_u < q_{umax}$ 

$$q_u - \frac{q_{cu}}{2} = \frac{nA_s f_y / \gamma_s}{hS}$$

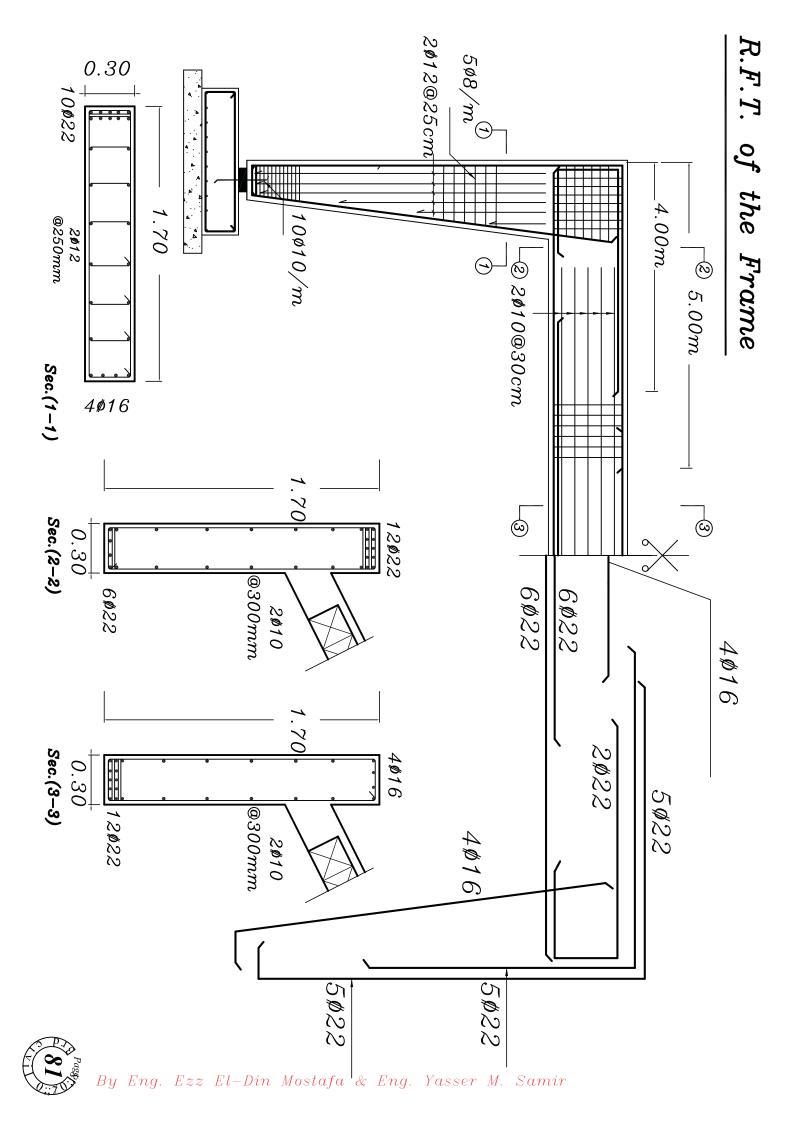
assume 
$$n=2$$

$$A_{s} = 78.5 mm^{2} = \emptyset 10$$

$$1.32 - \frac{0.98}{2} = \frac{2*78.5*240/1.15}{300*S} \implies S = 131.59mm$$

No. of 
$$stirrups/m' = \frac{1000}{S} = 7.6$$
 Take Stirrups 8010/m'

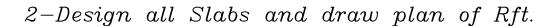




#### Example

For the given plan, it is required to:

1-Choose the suitable system to cover this Area.

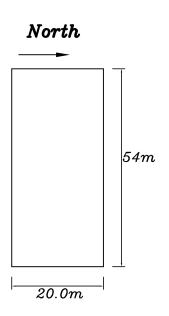


3-Design the main supporting element and draw details of Rft.

$$F.C. = 1.5kN/m^2$$
 ,  $L.L = 0.5 kN/m^2$ 

$$f_{cu} = 25 \ N/mm^2$$
,  $f_y = 360 \ N/mm^2$ 

Columns are only allowed on perimeter



#### Solution

$$t_{\rm s} = \frac{560}{24} = 23.33cm$$

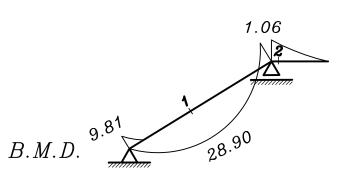
$$t_{s_{min}} = \frac{560}{35} = 16.00cm$$

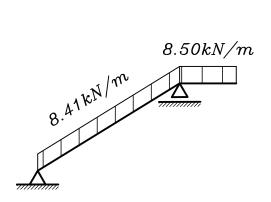
 $take t_S = 16 cm (Check def.)$ 

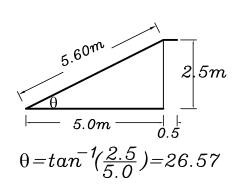
$$w_{su} = 1.4[t_s \gamma_c + F.c.] + 1.6 L.L.Cos\theta$$

$$w_{su} = 1.4[0.16*25+1.5]+1.6*0.5*0.89$$

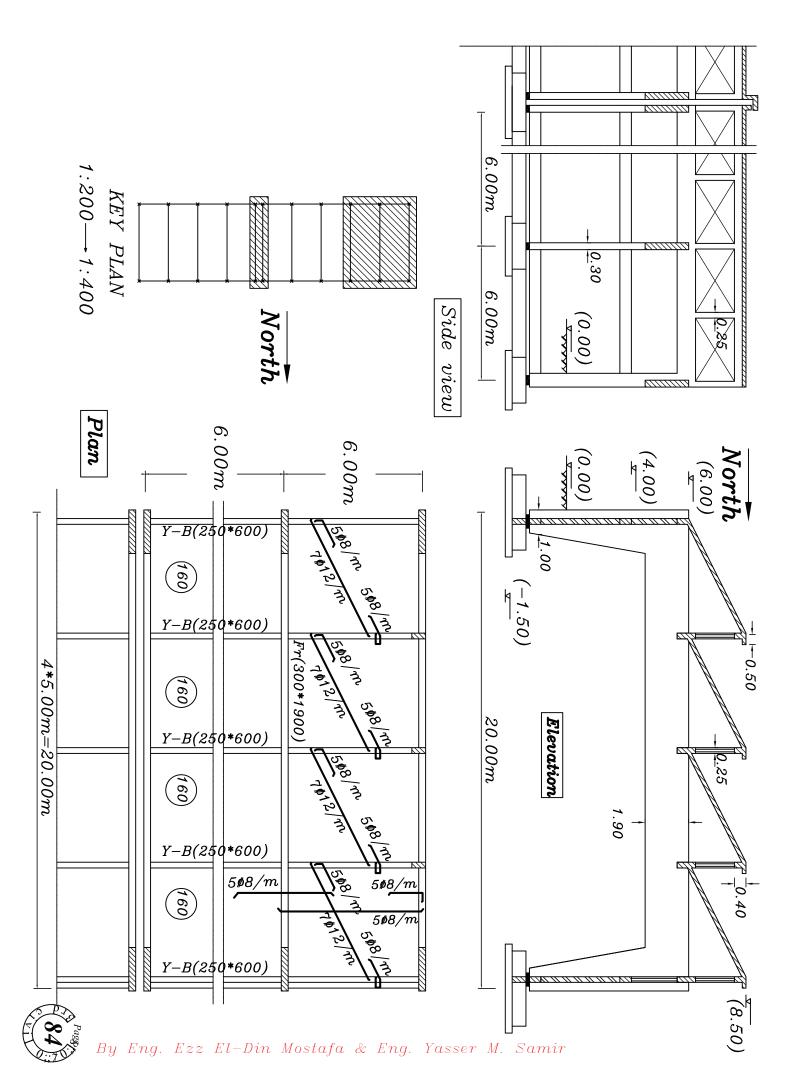
$$w_{su}$$
=8.41 $kN/m^2$ 







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Sec. 
$$(1-1)$$

$$140 = C_1 \sqrt{\frac{28.90*10^6}{1000*25}} \qquad C_1 = 4.12 \quad J = 0.807$$

$$A_s = \frac{28.90*10^6}{0.807*360*140} = 710 \text{mm}^2 / \text{m}^3$$

$$A_{s} = 7 \oplus 12/m'$$

Sec. 
$$(2-2)$$

$$A_s = 5 \oplus 8/m$$

# 2]Reactions of slabs on beams

$$\Sigma M_{\alpha} = 0$$

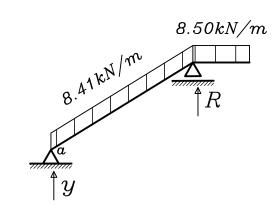
$$8.41*5.60*5.0/2+8.50*0.5*5.25=R*5.00$$

$$R=28.01kN/m$$

$$\Sigma y = 0$$

$$8.41*5.60+8.50*0.5=R+y$$

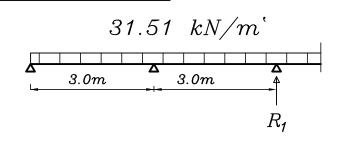
$$y = 23.34kN/m$$



## 3]Analysis of Ridge beam(250\*400)

$$w=R+o.w$$
  $kN/m$   
 $w=28.01+0.25*0.40*25*1.40$   
 $w=31.51$   $kN/m$ 

$$R_1 = 31.51*3.0 = 94.53kN$$



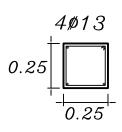
# 4]Design of Posts

$$R_p = R_1 + o.w$$
 of Post



$$R_p = 94.53 + 0.25*0.25*2.5.*25*1.40 = 100.00kN$$

$$100.00*10^3 = 0.35*250*250*25+0.67A_sf_y$$



$$A_s = -ve \longrightarrow A_s = 4 / 13$$

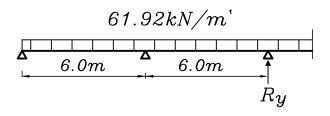
### 5]Design of of Y-beam

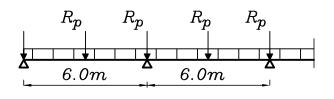
$$w_y = o.w. + y + \frac{\Sigma R_p}{Span} kN/m$$

$$w_y = 0.25*0.60*25*1.40+23.34+ \frac{2*100.0}{6.0}$$

$$w_y = 61.92 kN/m$$

$$R_y = 61.92*6.0 = 371.54 \ kN$$





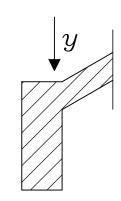
## 6]Analysis of End beam

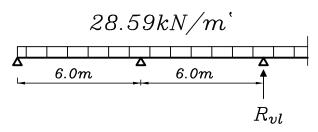
$$w_{vl.} = o.w + y$$
  $kN/m$ 

$$w_{vl.} = 0.25*0.60*25*1.40+23.34$$

$$w_{vl.} = 28.59 kN/m$$

$$R_{vl.} = 28.59*6.0=171.54kN$$



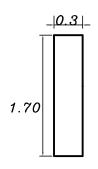




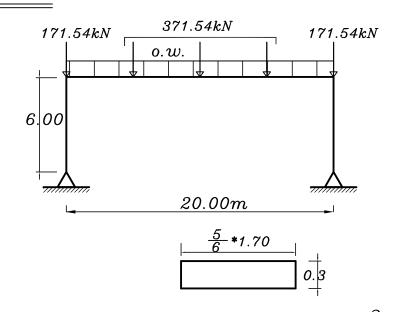
## 7]Design of Main system

$$0.w. = 0.30*1.70*25*1.40$$

$$o.w. = 17.85kN/m$$



$$I_b = 0.3 * \frac{1.7}{12} = 0.123 m^4$$



$$I_c = \frac{0.30*(\frac{5}{6} *1.70)^3}{12}$$

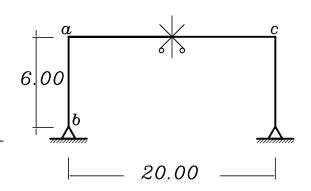
$$I_c = 0.071m^4$$

### For Joint $\alpha$

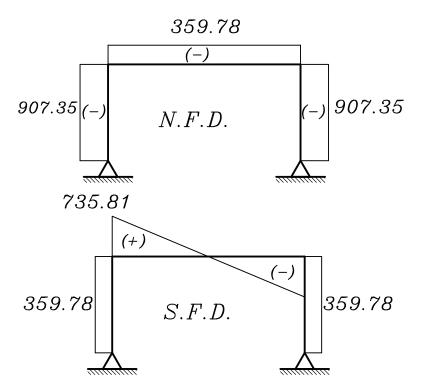
$$D.f_{ab} = \frac{0.75(I_c/h)}{(0.75\frac{I_c}{h}) + (0.5\frac{I_b}{L})}$$

$$D.f_{ab} = \frac{0.75*(0.071/6.00)}{0.75*(0.071/6.00)+0.50*(0.123/20)}$$

$$D.f_{ab} = 0.72$$







#### Design of Sections

Sec. 
$$(1-1)$$
  $M_{u,l} = 2158.67kN.m$   $N_{u,l} = 907.35kN.m$ 

$$N_{y,l} = 907.35kN.m$$

$$b=300mm$$
 ,  $t=1700mm$ 

$$300$$
 $N$ 
 $N$ 
 $1500$ 

$$\frac{N_{u.l.}}{btf_{cu}} = \frac{907.35*10^{3}}{300*1700*25} = 0.071>0.04 \text{ (Dont neglect } N_{u.l.}\text{)}$$

$$e = \frac{M_{u.l.}}{N_{u.l.}} = \frac{2158.67}{907.35} = 2.37m$$

$$\frac{e}{t} = \frac{2.37}{1.70} = 1.39 > 0.5$$
 (big eccentricity)

$$e_s = e + \frac{t}{2} - c = 2.37 + \frac{1.70}{2} - 0.1 = 3.12m$$

$$M_{us} = 907.35*3.12 = 2832.07kN.m$$

$$d = C_1 \sqrt{\frac{Mus}{b * f_{cu}}}$$

$$1600 = C_1 \sqrt{\frac{2832.07*10^6}{300*25}}$$
  $C_1 = 2.60 < 2.78$  take  $d = 1800mm$ 



$$e_{s} = e + \frac{t}{2} - c = 2.47 + \frac{1.90}{2} - 0.1 = 3.32m$$

$$M_{us} = 907.35*3.32 = 3012.40kN.m$$

$$1800 = C_1 \sqrt{\frac{3012.40*10^6}{300*25}} \qquad C_1 = 2.84 \& J = 0.72$$

$$A_{\rm S} = \frac{{\it Mus}}{{\it J.d.f_y}} \ - \frac{{\it Nus}}{{\it f_y}/\gamma_{\rm S}}$$

$$A_s = \frac{30124.40*10^6}{0.72*1800*360} - \frac{907.35*10^3}{360/1.15}$$

$$A_s = 35.18 cm^2 = 10022$$

Sec. (2-2) 
$$M_{u.l.} = 2158.67kN.m$$
  $N_{u.l.} = 359.78kN.m$ 

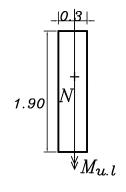
b=300mm . t = 1900mm

$$\frac{N_{u.l.}}{btf_{cu}} = \frac{359.78*10^{3}}{300*1900*25} = 0.025<0.04 \ (neglect \ N_{u.l.})$$

$$d=C_1\sqrt{\frac{Mu.l.}{b*f_{cu}}}$$

$$1800 = C_1 \sqrt{\frac{2158.67*10^6}{300*25}} \qquad C_1 = 3.36 \& J = 0.77$$

$$C_1 = 3.36 \& J = 0.77$$



$$A_{s} = \frac{2158.67*10^{6}}{0.77*1800*360}$$

$$A_s = 43.16 cm^2 = 12022$$

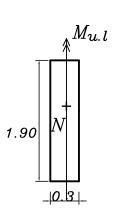
Sec. 
$$(3-3)$$
  $M_{u.l.} = 2449.23kN.m$   $N_{u.l.} = 359.78kN.m$ 

$$b=300mm$$
 ,  $t=1900mm$ 

$$d = C_1 \sqrt{\frac{Mu.l.}{b*f_{cu}}}$$

$$1800 = C_1 \sqrt{\frac{2449.23*10^6}{300*25}}$$

$$C_1 = 3.15 \& J = 0.76$$



$$A_s = \frac{2449.23*10^6}{0.76*1800*360}$$

$$A_s = 49.96 \, \text{cm}^2 = 11025$$

#### Check Shear

$$Q_{cr} = Q_{max} - w(\frac{c}{2} + \frac{d}{2})$$

$$Q_{cr} = 735.81 - 17.85 \left( \frac{1.90}{2} + \frac{1.80}{2} \right)$$

$$Q_{cr} = 702.79kN$$

$$q_{su} = \frac{Q_{cr}}{bd} = \frac{702.79*10^3}{300*1800} = 1.31 \text{ N/mm}^2$$

$$q_{cu} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 \ N/mm^2$$

$$q_{max} = 0.7 \sqrt{\frac{25}{1.5}} = 2.86 \text{ N/mm}^2$$

$$q_{cu} < q_u < q_{umax}$$

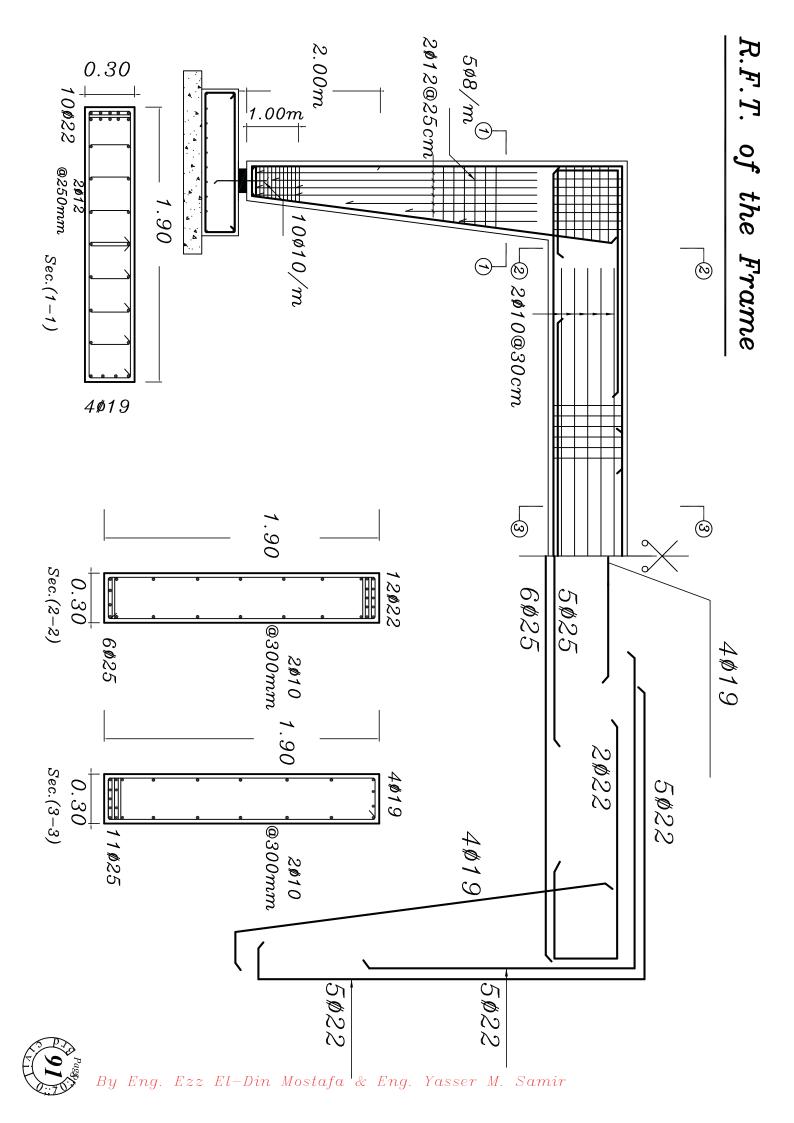
$$q_u - \frac{q_{cu}}{2} = \frac{nA_s f_y / \gamma_s}{bS}$$

assume 
$$n=2$$

$$A_{s} = 78.5 mm^{2} = \emptyset 10$$

$$1.31 - \frac{0.98}{2} = \frac{2*78.5*240/1.15}{300*S} \implies S = 133.19mm$$

No. of stirrups/m'= 
$$\frac{1000}{S}$$
 = 7.5 Take Stirrups 8010/m'



#### Example

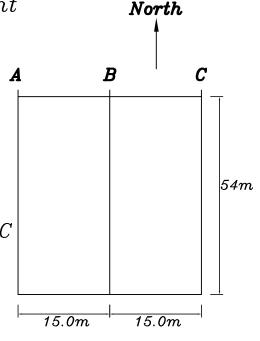
For the given plan, it is required to:

- 1-Choose the suitable system to cover this Area.
- 2-Design all Slabs and draw plan of Rft.
- 3-Design the main supporting element and draw details of Rft.

$$F.C. = 1.5kN/m^2$$
 ,  $L.L = 0.5 kN/m^2$ 

$$f_{cu}$$
=32.5 N/mm<sup>2</sup>,  $f_y$  =360 N/mm<sup>2</sup>

Columns are only allowed on axes A,B,C

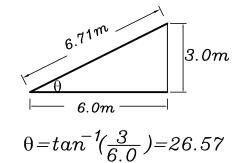


### Solution

Use continuous frame

$$t = \frac{671}{16} = 41.94cm$$

 $take \ t=25 \ cm \ [20cm+5cm]$ 



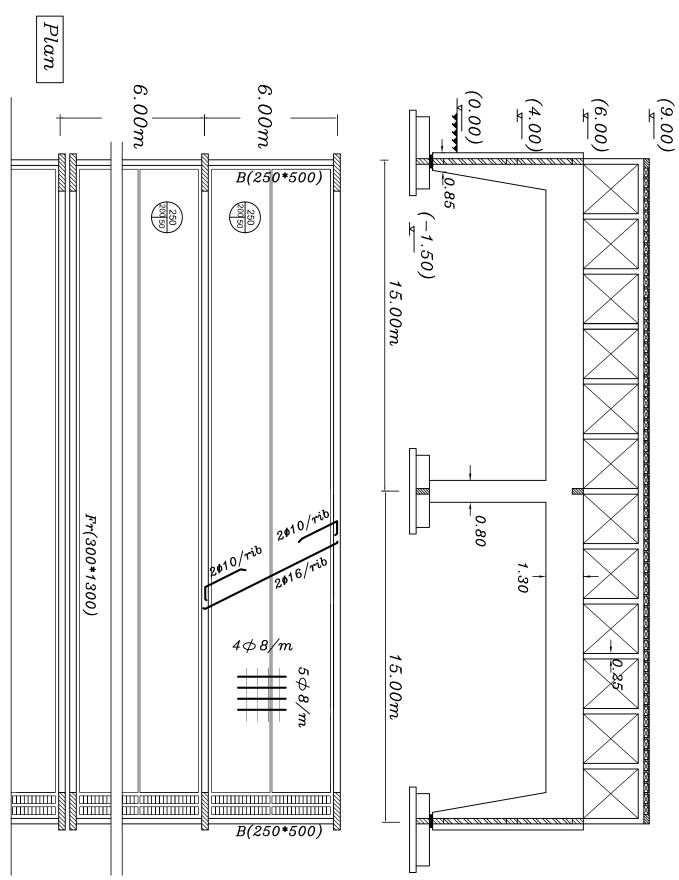
$$w_{su}=1.4(t_s\gamma_c+F.C.+2bh\gamma_c+10*wt.of\ block]+1.6L.L.Cos\theta$$
  
 $w_{su}=1.4(0.05*25+1.5+2*0.1*0.2*25+10*0.15]+1.6*0.5*0.89$   
 $w_{su}=8.06kN/m^2$ 

$$w_{su/Rib} = 0.5*8.06 = 4.03kN/m$$

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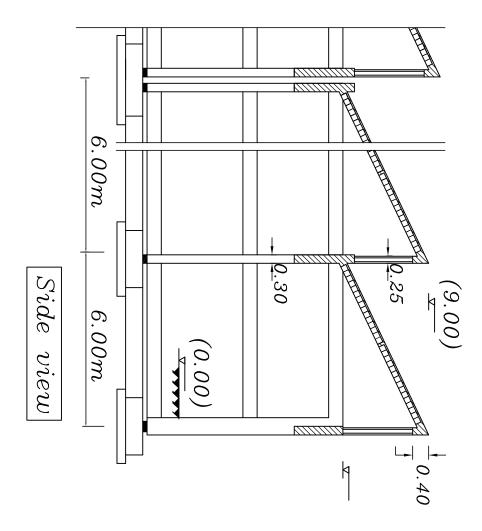


Elevation

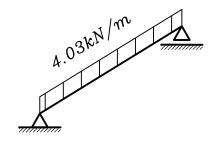




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Sec. (1-1)

$$220 = C_1 \sqrt{\frac{20.28*10^6}{500*25}}$$

$$C_1 = 5.46$$
  $J = 0.826$ 

$$A_{s} = \frac{20.28*10^{6}}{0.826*360*220} = 3.10cm^{2}/rib$$

$$A_s = 2 \oplus 16/rib$$

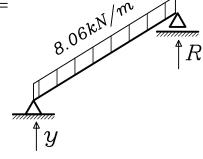
Sec. 
$$(2-2)$$

$$A_s = 2 \oplus 10/rib$$

# 2]Reactions of slabs on beams

$$R = y = w_{su} - L$$
  $kN/m$ 

$$R=y=8.06*6.71/2=27.04 \ kN/m$$

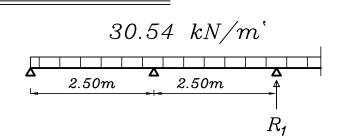


# 3]Analysis of Ridge beam(250\*400)

$$w=R+o.w$$
  $kN/m$   
 $w=27.04+0.25*0.40*25*1.40$ 

$$w=30.54 \text{ kN/m}$$

$$R_1 = 30.54*2.5 = 76.35kN$$



## 4]Design of Posts

$$R_p = R_1 + o.w$$
 of Post

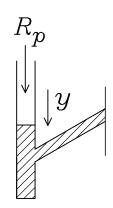


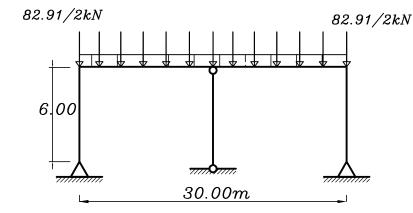
## 5]Design of main system

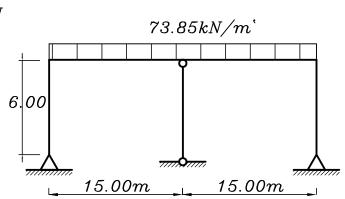
### (Y-beam) هو نفسه (Frame) لاحظ في هذه الحالة يكون

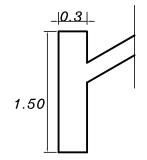
لان الشكل متماثل يمكن اعتبار العمود الاوسط Link member

$$w_f = 0.w. + y + \frac{\Sigma R_p}{Span}$$
  $kN/m$   $w_f = 0.30*1.30*25*1.40+27.04+ \frac{12*82.91}{20.0}$   $w_f = 73.85kN/m$ 









$$I_b = 0.3 * \frac{1.3}{12} = 0.055 m^4$$

$$I_{c} = \frac{0.30*(\frac{5}{6}*1.30)^{3}}{12}$$

$$I_{c} = 0.032m^{4}$$

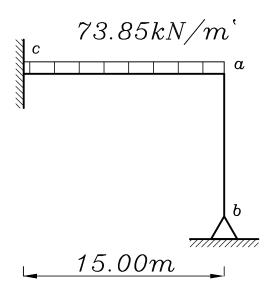
#### For Joint a

$$D.f_{ab} = \frac{0.75(I_c/h)}{(0.75\frac{I_c}{h}) + (\frac{I_b}{L})}$$

$$D.f_{ab} = \frac{0.75*(0.032/6.00)}{0.75*(0.032/6.00) + (0.055/15)}$$

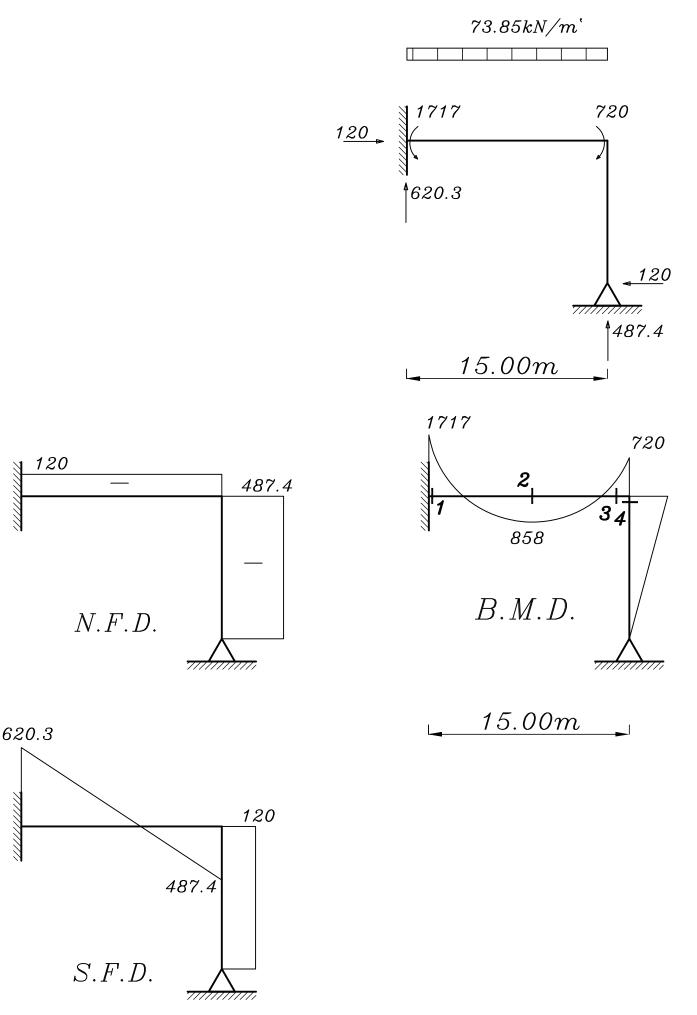
$$D.f_{ab} = 0.52$$
  $D.f_{ac} = 1 - 0.52 = 0.48$   $F.E.M. = 73.85*15^{2}/12 = 1384.7$   $kN.m$ 

يحل نصف الـ Frame لانه متماثل



Joint	С	a	
member	ca	ac	ab
D.F.		0.48	0.52
F.E.M.	1384.7	-1384.7	0.0
Bal. M	0.0 *0.5	*°°° 664.7	720
C.O.M.	332.3	0.0	0.0
Bal. M	0.0	0.0	0.0
$m{M}_{final}$	1717	-720	720





Sec. 
$$(1-1)$$

Sec. (1-1)  $M_{u.l.} = 1717kN.m$ 

 $N_{u,l} = 120kN$ 

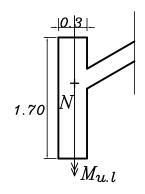
b=300mm , t=1300mm

$$\frac{N_{u.l.}}{btf_{cu}} = \frac{120*10^3}{300*1300*25} = 0.009<0.04 \ (neglect \ N_{u.l.})$$

$$d = C_1 \sqrt{\frac{Mu.l.}{b * f_{cu}}}$$

$$1200 = C_1 \sqrt{\frac{1717*10^6}{300*32.5}}$$

$$C_1 = 2.85 \& J = 0.74$$



$$A_{s} = \frac{1717*10^{-6}}{0.74*1200*360}$$

$$A_s = 5371 \, mm^2 = 11025$$

Sec. 
$$(2-2)$$
  $M_{u.l.} = 858kN.m$ 

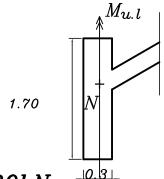
$$N_{u.l.} = 120kN$$
 $neglected$ 

$$1200 = C_1 \sqrt{\frac{858*10^{-6}}{300*32.5}}$$

$$C_1 = 4.0 \& J = 0.8$$

$$A_{s} = \frac{1924.06*10^{6}}{0.76*1600*360}$$

$$A_s = 2483 mm^2 = 7022$$



Sec. 
$$(3-3)$$
  $M_{u.l.} = 720kN.m$ 

$$A_s = 6$$
  $\emptyset 22$ 

 $N_{u.l.} = 120kN$ neglected



Sec. 
$$(4-4)$$

$$\frac{Sec. (4-4)}{M_{u,l}} = 720kN.m$$

$$N_{u,l} = 487.4kN$$

$$\frac{N_{u.l.}}{btf_{cu}} = \frac{120*10^3}{300*1300*25} = 0.038<0.04 \ (neglect N_{u.l.})$$

$$A_s = 6 \emptyset 22$$

#### Check Shear

$$Q_{cr} = Q_{max} - w(\frac{c}{2} + \frac{d}{2})$$

$$Q_{cr} = 620.3 - 73.85 \left( \frac{0.80}{2} + \frac{1.20}{2} \right)$$

$$Q_{cr} = 546.45kN$$

$$q_{su} = \frac{Q_{cr}}{bd} = \frac{546.45*10^3}{300*1200} = 1.52 \text{ N/mm}^2$$

$$q_{cu} = 0.24 \sqrt{\frac{32.5}{1.5}} = 1.12 \text{ N/mm}^2$$

$$q_{max} = 0.7 \sqrt{\frac{32.5}{1.5}} = 3.25 \ N/mm^2$$

$$q_u - \frac{q_{cu}}{2} = \frac{nA_s f_y / \gamma_s}{bS}$$

assume n=2

$$A_{s} = 78.5 mm^{2} = \emptyset 10$$

$$1.52 - \frac{1.12}{2} = \frac{2*78.5*240/1.15}{300*S} \implies S = 113mm$$

No. of 
$$stirrups/m' = \frac{1000}{S}$$

Take Stirrups 9010/m'

 $q_{cu} < q_u < q_{umax}$ 



#### Design of Internal column

$$N_{u,l} = 620.3*2 = 1240.6kN$$

$$\lambda_{b_{in}} = \frac{1.3*5.45}{0.8} = 8.8$$
,  $\lambda_{b_{out}} = \frac{1.2*6.25}{0.3} = 25$  unsafe

$$Take \quad b_{col} = 35cm$$

$$\lambda_{b_{out}} = \frac{1.2*6.25}{0.35} = 21.4$$

Column is Long outside plan.

$$\delta_b = \frac{\lambda_{bout}^2 * b}{2000} = \frac{21.4 * 0.35}{2000} = 0.08 \ m$$

$$M_{add} = P.\delta_b = 1240.6*0.08 = 99kN.m$$

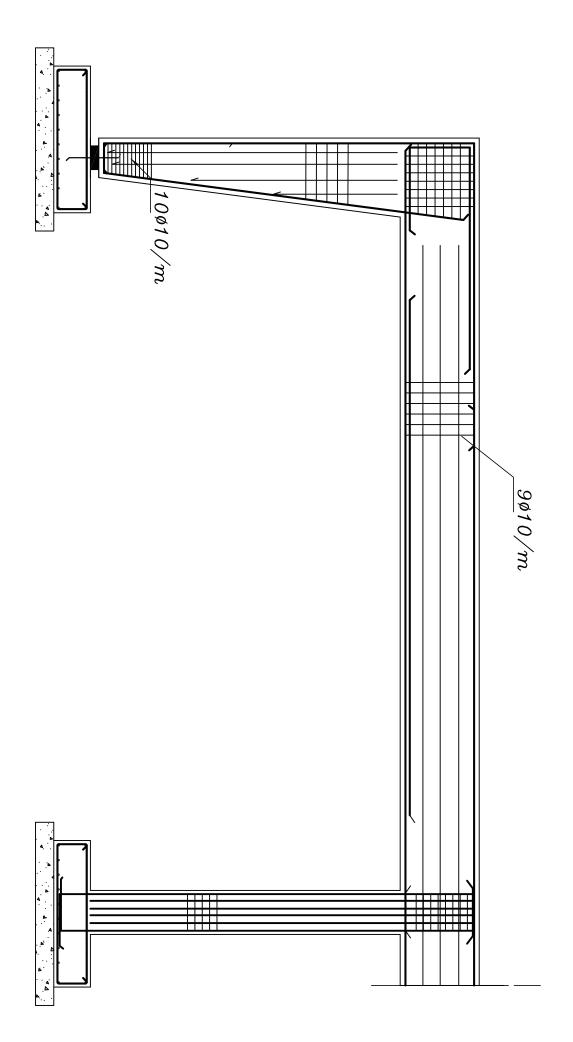
$$\frac{N_{u.l.}}{btf_{cu}} = \frac{1240.6*10^3}{350*800*32.5} = 0.136 , \frac{M_{u.l.}}{b^2 tf_{cu}} = \frac{99*10^6}{350^2*800*32.5} = 0.03$$

$$\rho_{<1}$$
 Take  $\rho_{=1}$ 

$$A_{s_{min}} = \frac{0.25 + 0.052 * 21.4}{100} * 350 * 800 = 3816 mm^{2}$$

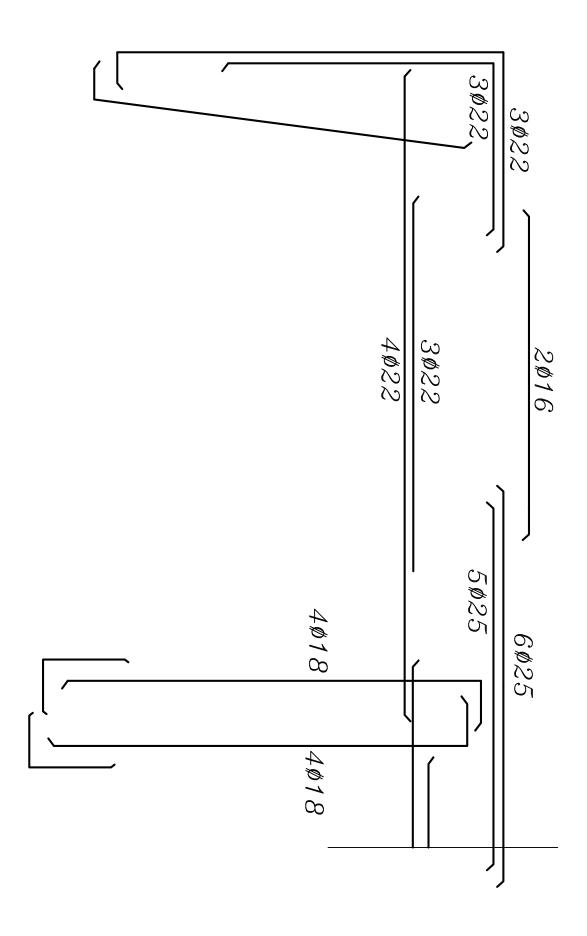
$$16 \, \oplus 18$$







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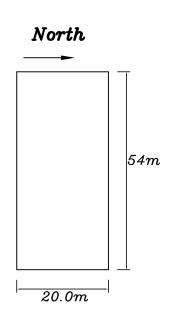
#### Example

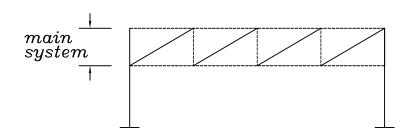
For the given plan, it is required to:

- 1-Choose the suitable system to cover this Area.
- 2-Design all Slabs and draw plan of Rft.
- 3-Design the main supporting element and draw details of Rft.

$$F.C. = 1.5kN/m^2$$
 ,  $L.L = 0.5 kN/m^2$ 

$$f_{cu} = 25 \text{ N/mm}^2$$
,  $f_y = 360 \text{ N/mm}^2$ 

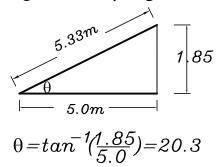


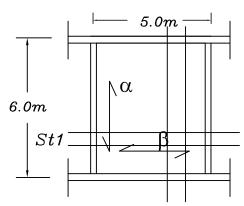


Columns are only allowed on perimeter

Two way slab

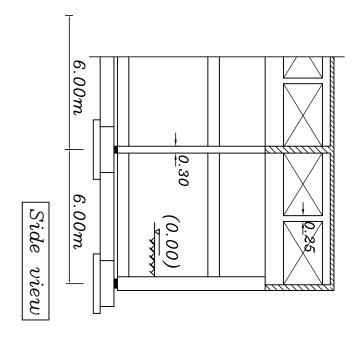
لاحظ ان البلاطة تحل على انها

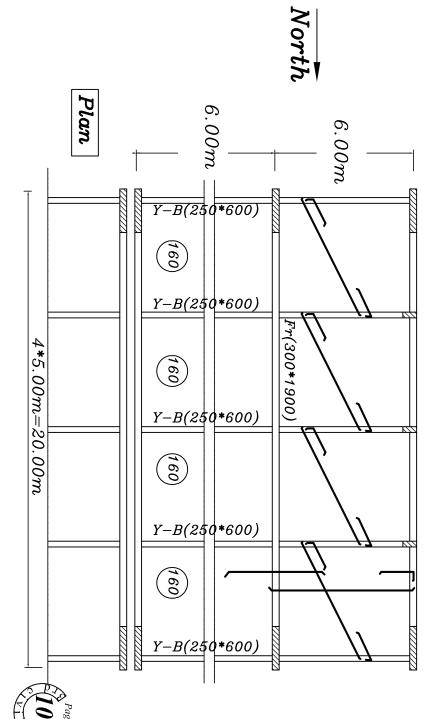


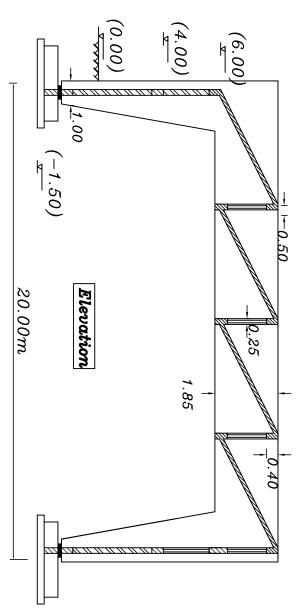


$$r = \frac{0.76*6.0}{5.33} = 0.85$$
 $r = 1.17$ 
 $\alpha = 0.43$ 
 $\beta = 0.25$ 



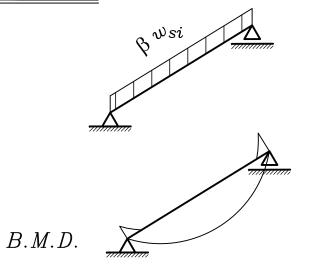




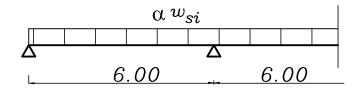


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### Strip 1

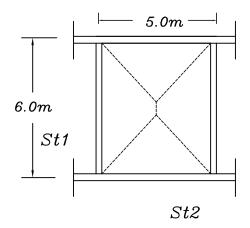


## Strip 2





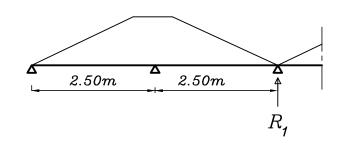
### Load distribution

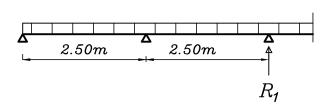


# Analysis of Ridge beam(250\*400)

$$w = o.w. + \frac{\Sigma Area}{Span} w_{si}$$

$$R_1 = w * 2.5 = ----kN$$





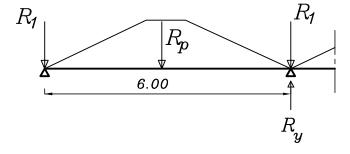


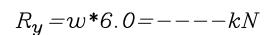
## Design of Posts

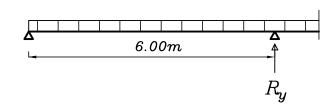
$$R_p = R_1 + o.w$$
 of  $Post$ 

### Analysis of Y-beam

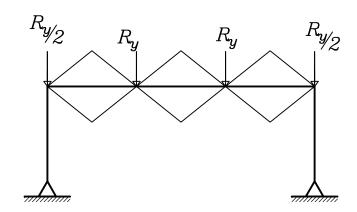
$$w = 0.w. + \frac{\Sigma Area}{Span} w_{si} + \frac{R_1 + R_p}{Span}$$







### Analysis of Frame



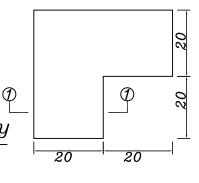
ثم يتم تصميم ال Frame كما سبق



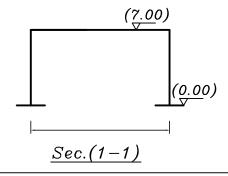
#### Example

For the given plan and cross- section,

Columns are allowed on the perimeter only it is required to:

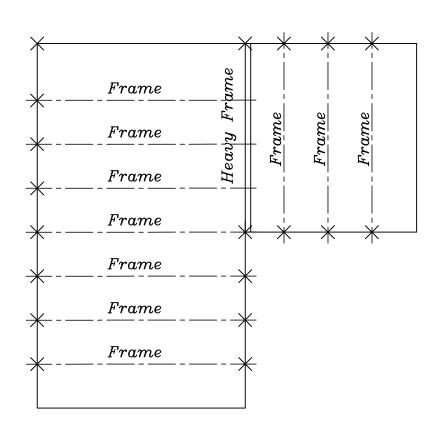


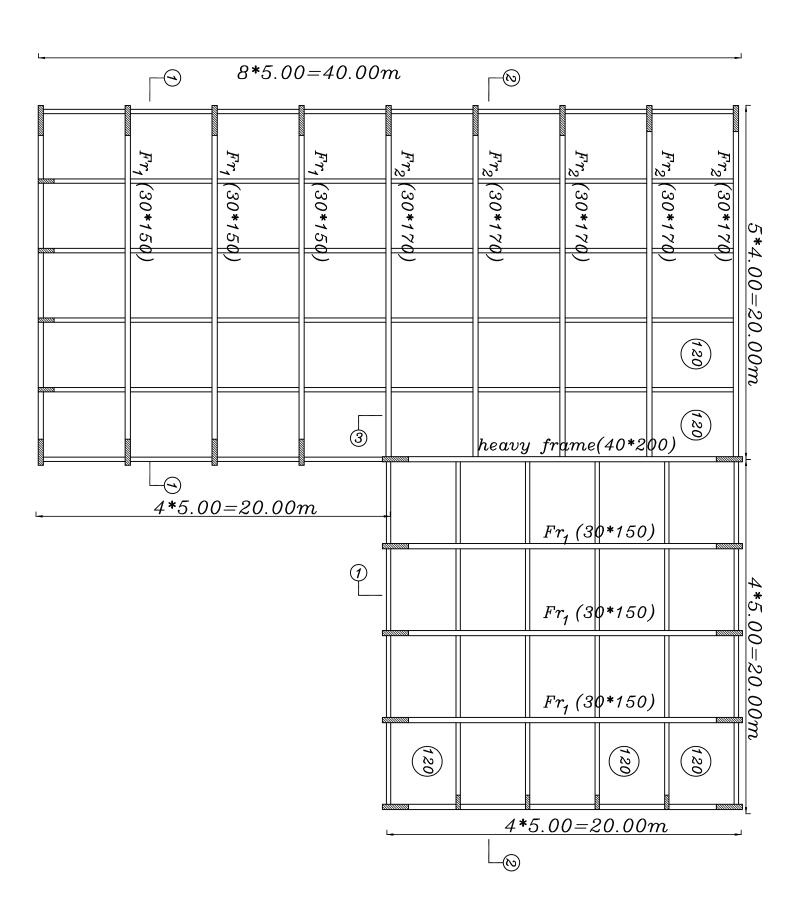
1- Draw structural plan and cross
section to show all concrete elements.
2- Show How to solve main systems

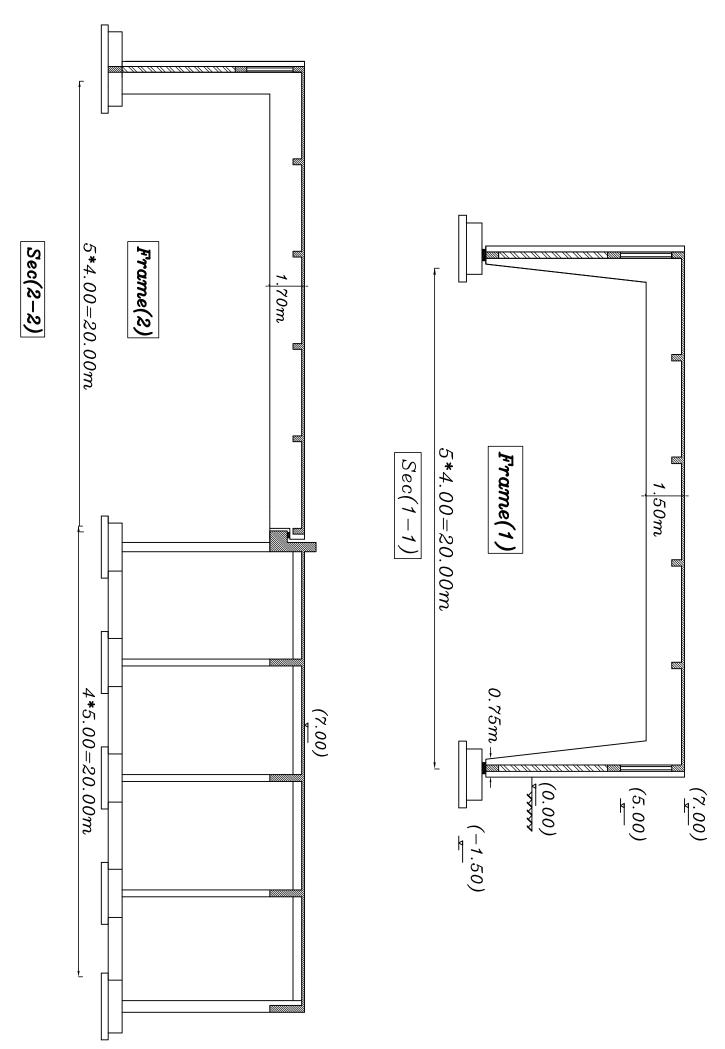


#### Solution

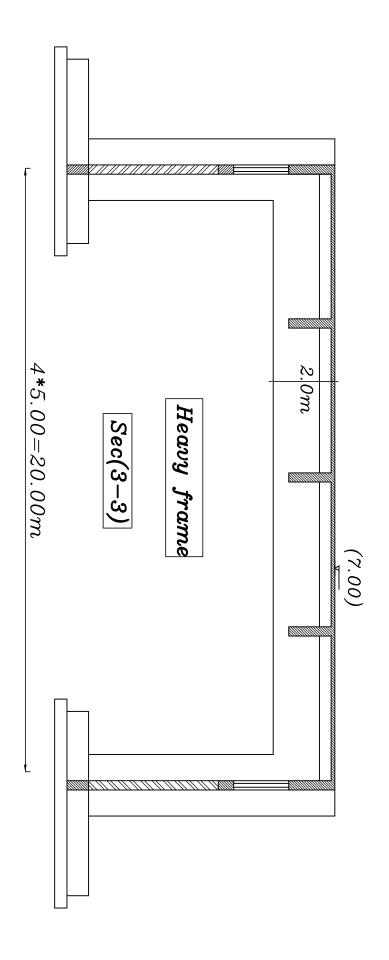
لاحظ ان الارض ليست مستطيلة



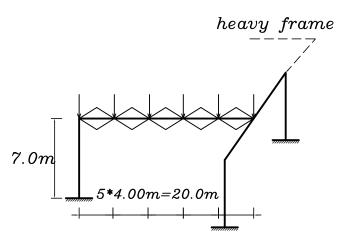




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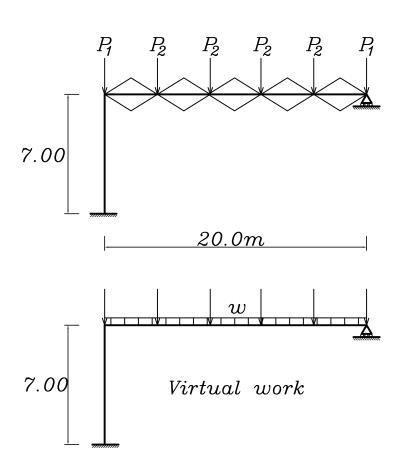


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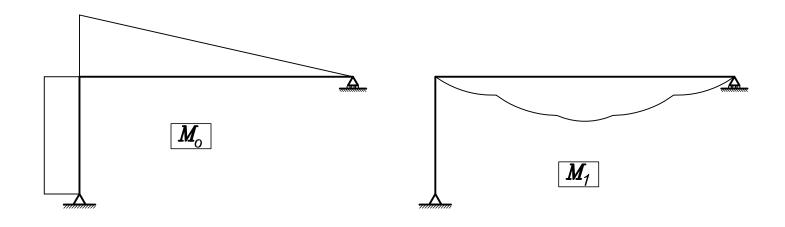


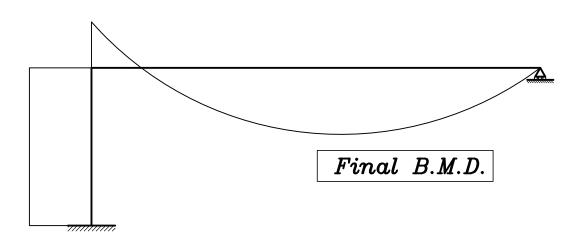
# For Frame(2)

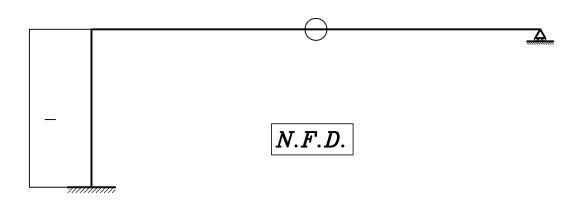
المفروض يتم حله فى الفراغ (Space frame) ولكن نظرا لصعوبة الحل يتم وضعه على (Neoprane plate) وبالتالى يصبح



## Solving using virtual work method

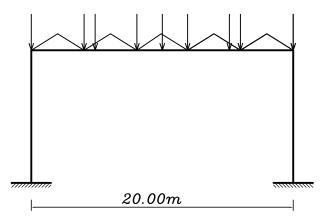






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#### For heavy frame



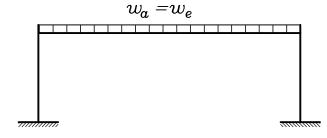
نتيجة لان (heavy frame) عليه أحمال ثقيلة فان

$$b=40cm$$
,  $t=\frac{L}{10} = \frac{20}{10} = 2.00m$ 

$$w_a = w_e = \gamma_c b(t - t_s) * 1.40 + \frac{\sum Area}{Span} w_s + \frac{\sum Concentrated loads}{Span}$$

Where Concentrated loads are the loads from secondary

Beams & Frames



ثم نحله باستخدام (Moment Distribution)

